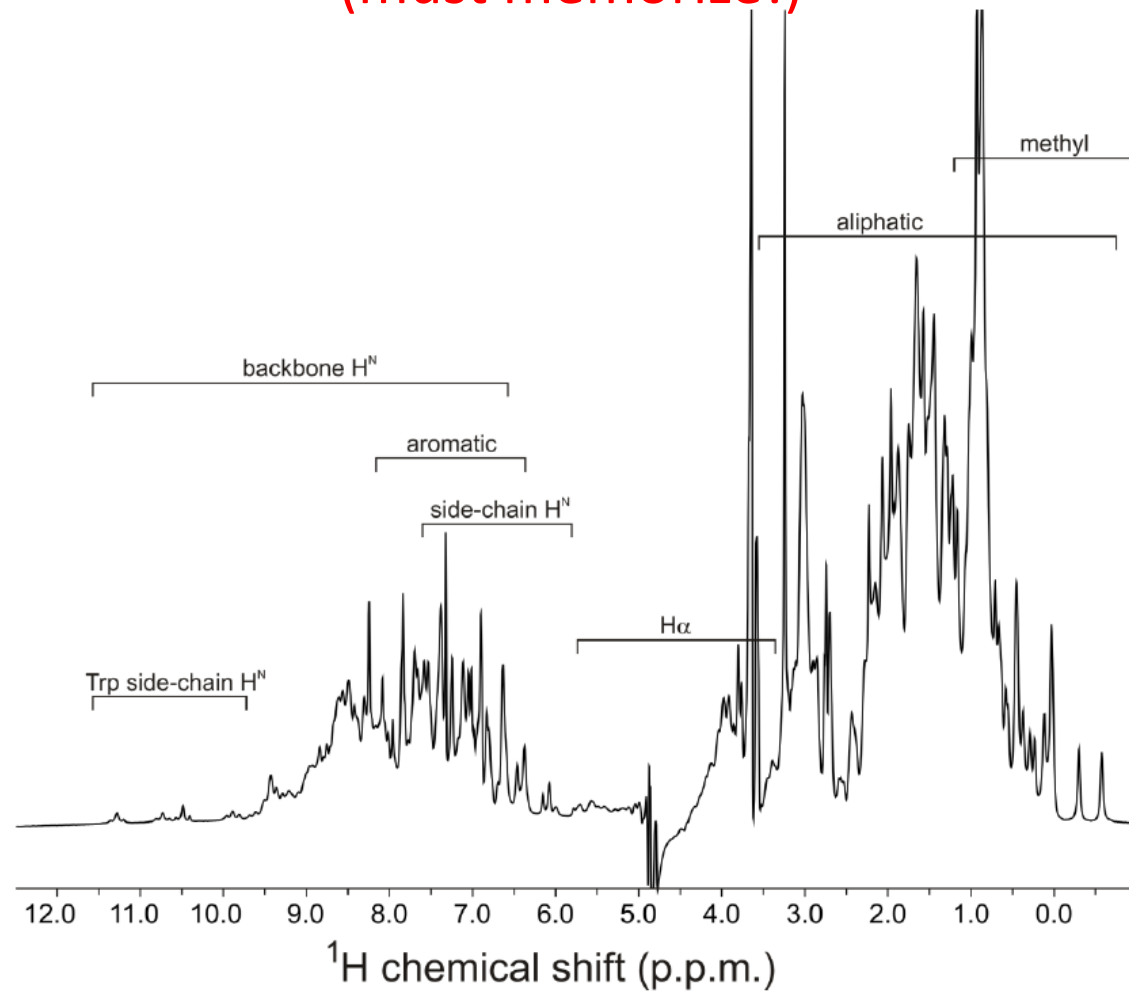


# Protein $^1\text{H}$ Chemical Shifts

(must memorize!)



From "Peptide Resonance Assignments."

Girvin, M, AECOM, Course 1022

# Protein $^1\text{H}$ Chemical Shifts

Typical proton chemical shifts for amino acids within a protein.

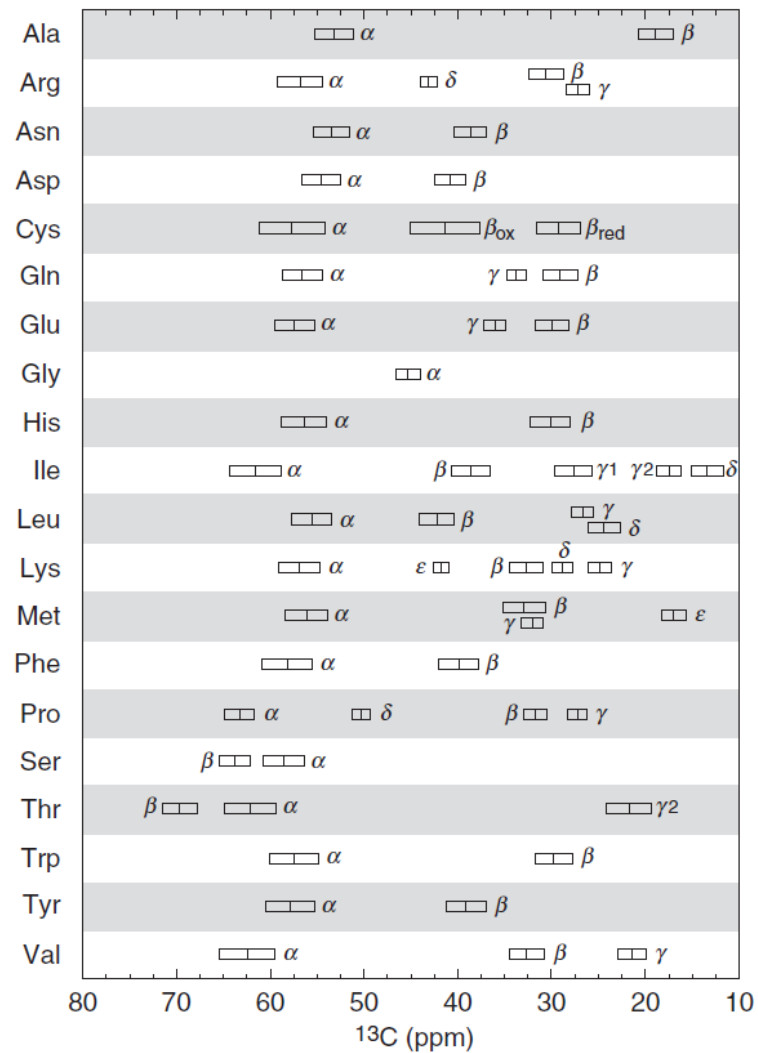
---

type	HN	HA	HB	other
gly	8.0	4.2,3.8		
ala	8.0	4.4	1.4 $\beta$	
val	8.0	4.4	2.0 $\beta$	1.0, 0.9 $\gamma$
ser	8.0	4.5	3.7, 3.6 $\beta$	
thr	8.0	4.5	4.4 $\beta$	1.2 $\gamma$
cys	8.0	4.5	3.3, 3.1 $\beta$	
asp	8.0	4.6	2.5, 2.3 $\beta$	

---

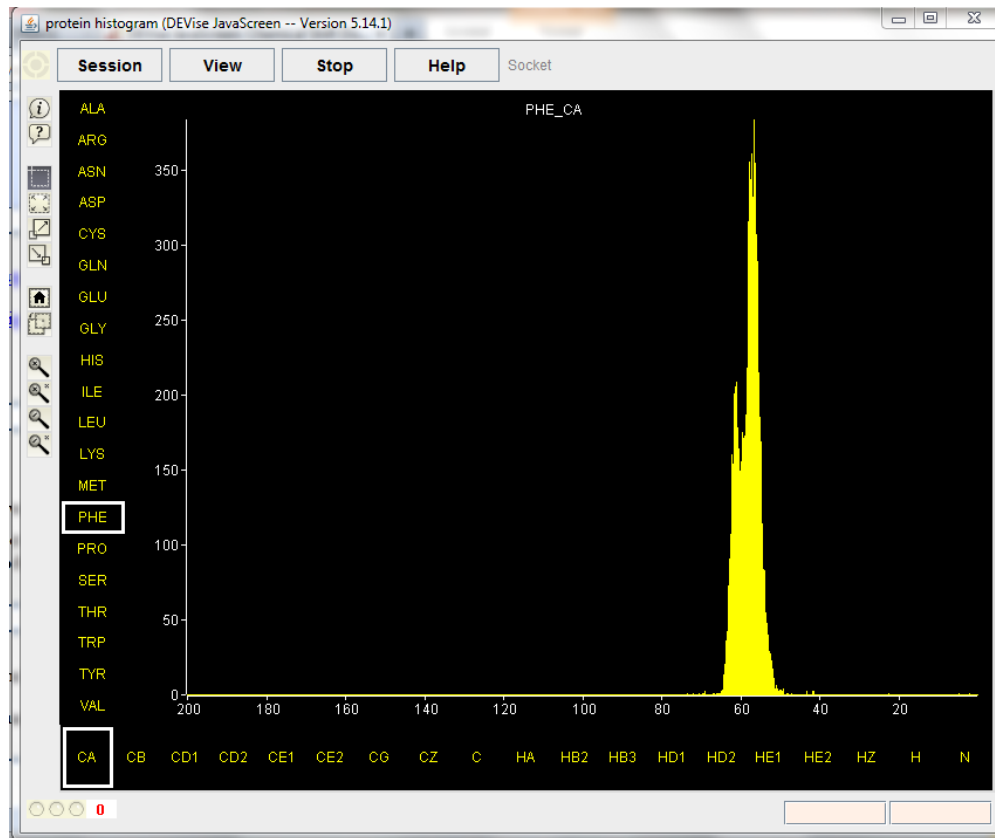
- Excerpt from:  
[http://hoffman.cm.utexas.edu/research/h\\_cs.pdf](http://hoffman.cm.utexas.edu/research/h_cs.pdf)

# Protein $^{13}\text{C}$ Chemical Shifts



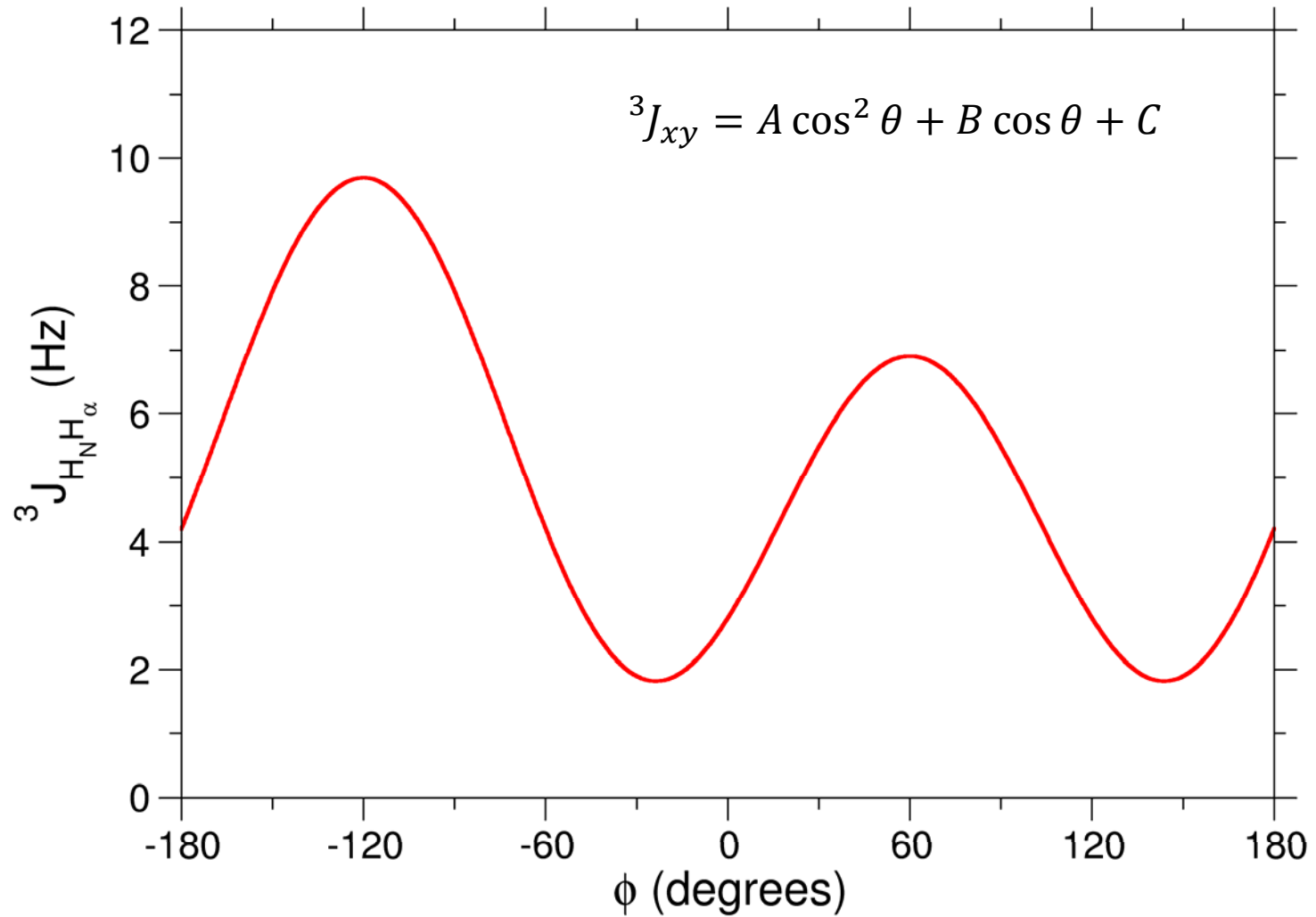
From *Protein NMR Spectroscopy*  
Cavanagh, et al., Chapt. 10, p. 795

# DEVise Chemical Shift Viewer



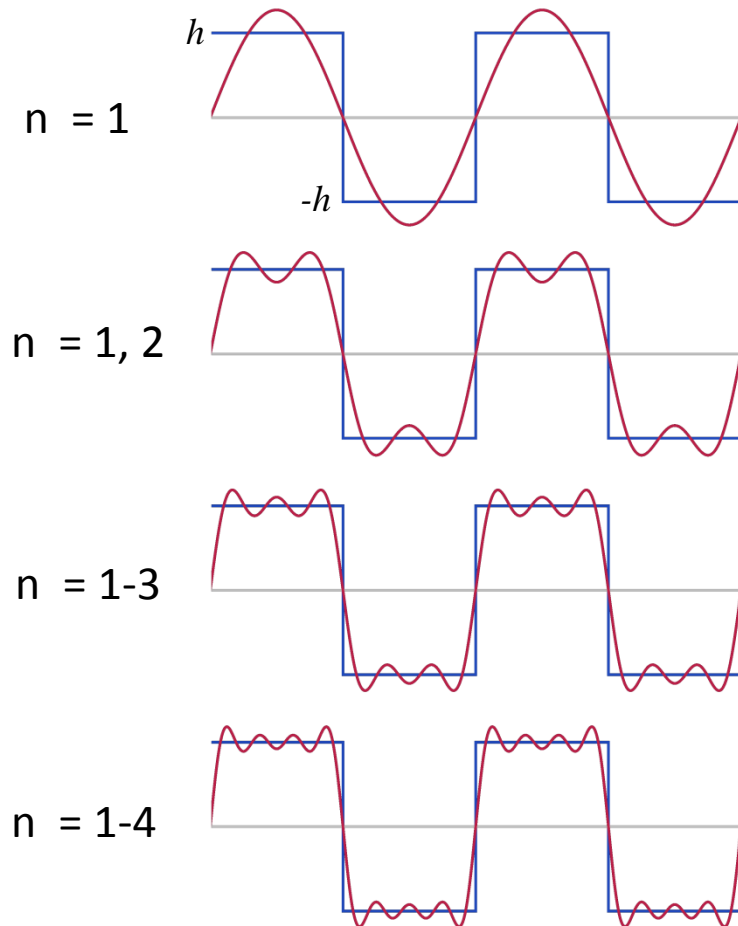
- Available at the BMRB:  
[http://www.bmrwisc.edu/ref\\_info/](http://www.bmrwisc.edu/ref_info/)

# Karplus Equation



# Fourier Transforms: Periodic Functions

(with period  $2\pi$ )



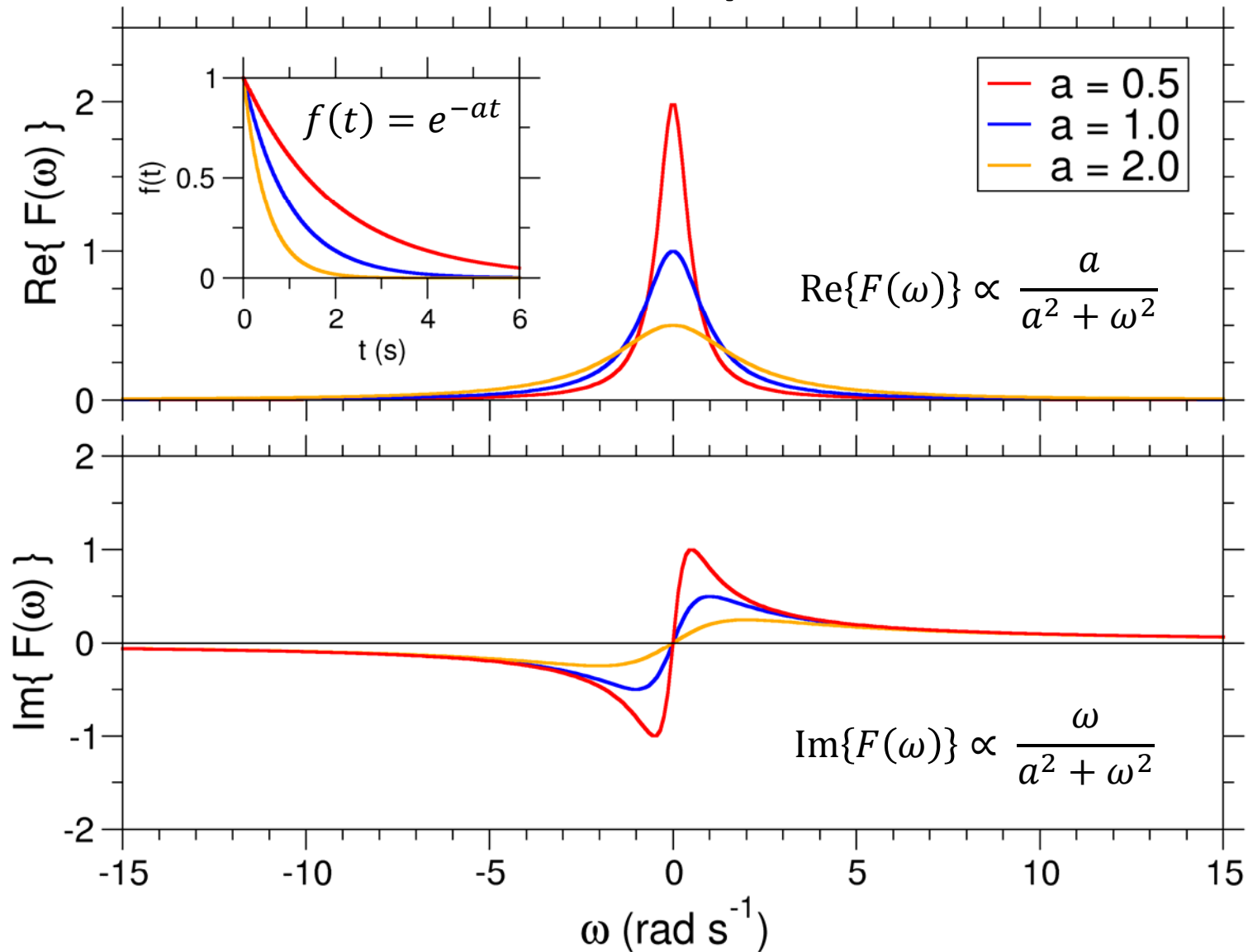
$$f(t) = \frac{a_0}{2} + \sum_{n=1}^{\infty} [a_n \cos(nt) + b_n \sin(nt)]$$

$$a_n = \frac{1}{\pi} \int_{-\pi}^{\pi} f(t) \cos(nt) dt$$

$$b_n = \frac{1}{\pi} \int_{-\pi}^{\pi} f(t) \sin(nt) dt$$

$$f(t) = \frac{4h}{\pi} \left( \frac{\sin t}{1} + \frac{\sin 3t}{3} + \dots \right)$$

# Fourier Transform: Exponential Decay



# Summary

## Chemical Shifts and J-Coupling

- Chemical shifts allow comparison of NMR frequencies at different fields
- Chemical shifts are different depending on environment and nucleus type
- Scalar coupling gives rise to multiple signals for nuclei that are electronically coupled (independent of  $B_0$ )



# Summary

## Fourier Transforms

- Any function can be represented by a sum of periodic functions with different frequencies
- Fourier transforms tell you the contribution of each frequency to the sum above
- NMR signals can be built up from sines, cosines, and decays. These all have characteristic transforms; Faster decay  $\rightarrow$  broader peak.
- The product of two time domain functions ( $e^{-at} \sin(\omega t)$ ) results in a convolution of their Fourier transforms. The signals are “mixed.”