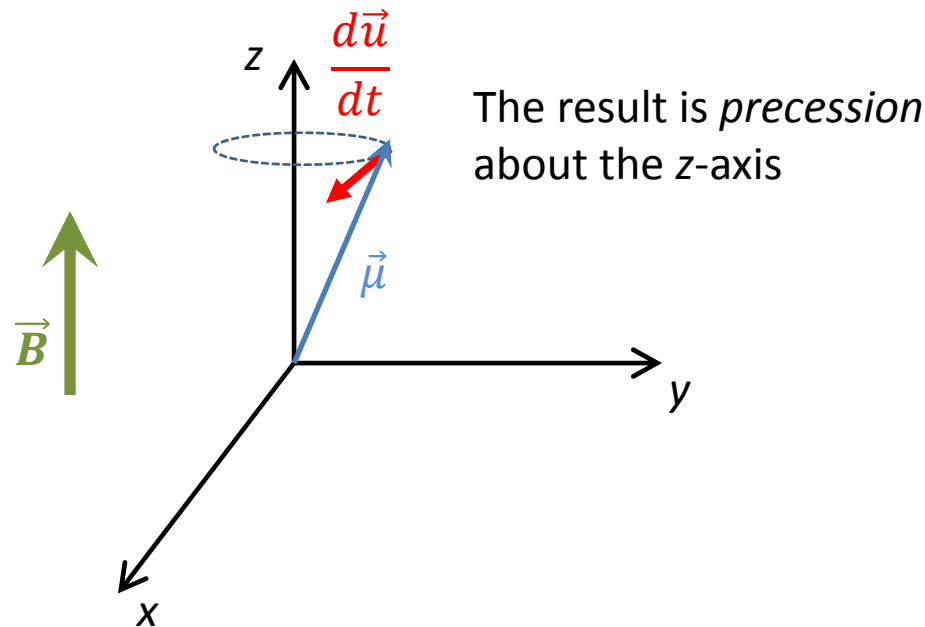


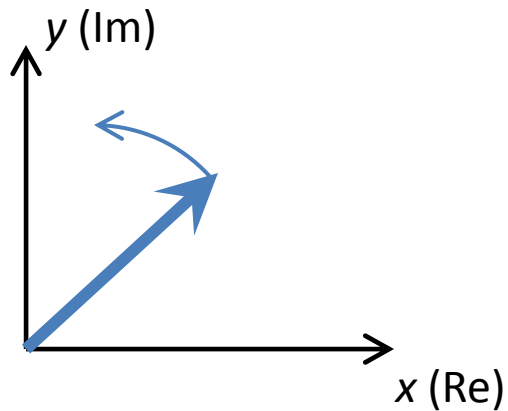
# Why Fourier Transforms?

- In a magnetic field, individual nuclear spins feel a torque, and  $\frac{d\vec{\mu}}{dt} = \gamma\vec{\mu} \times \vec{B}$

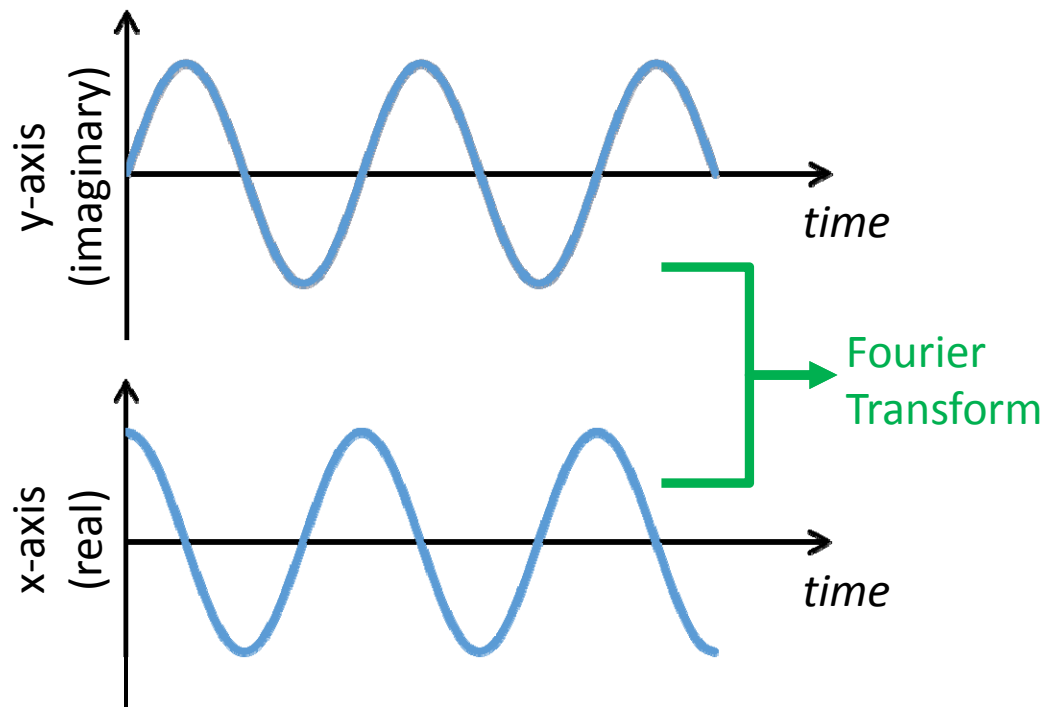


# Larmor Precession

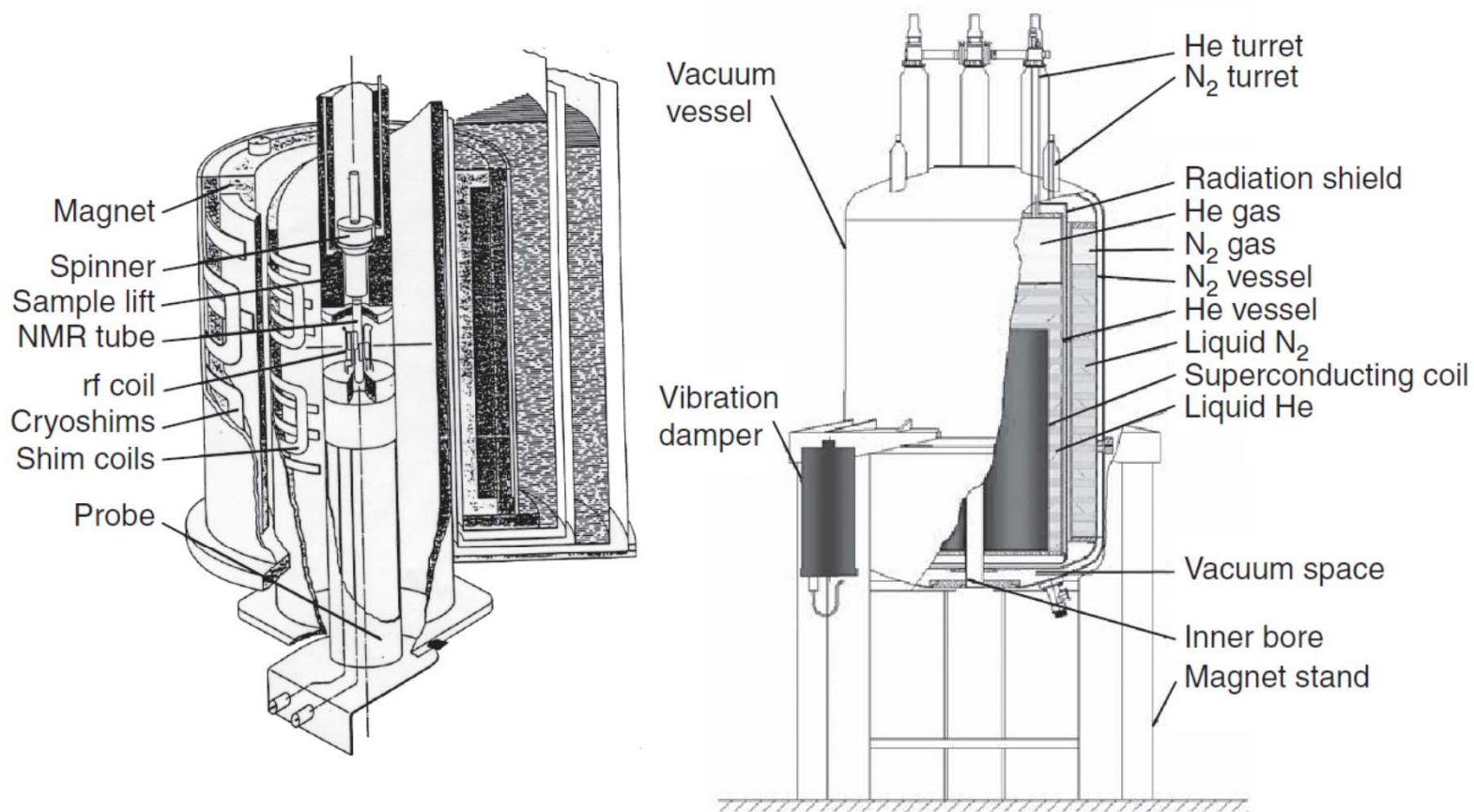
- When excited, spins will precess at the Larmor frequency,  $\omega = \gamma B_0$ . This is identical to the absorption frequency.



We detect magnetization as it precesses in the sample.

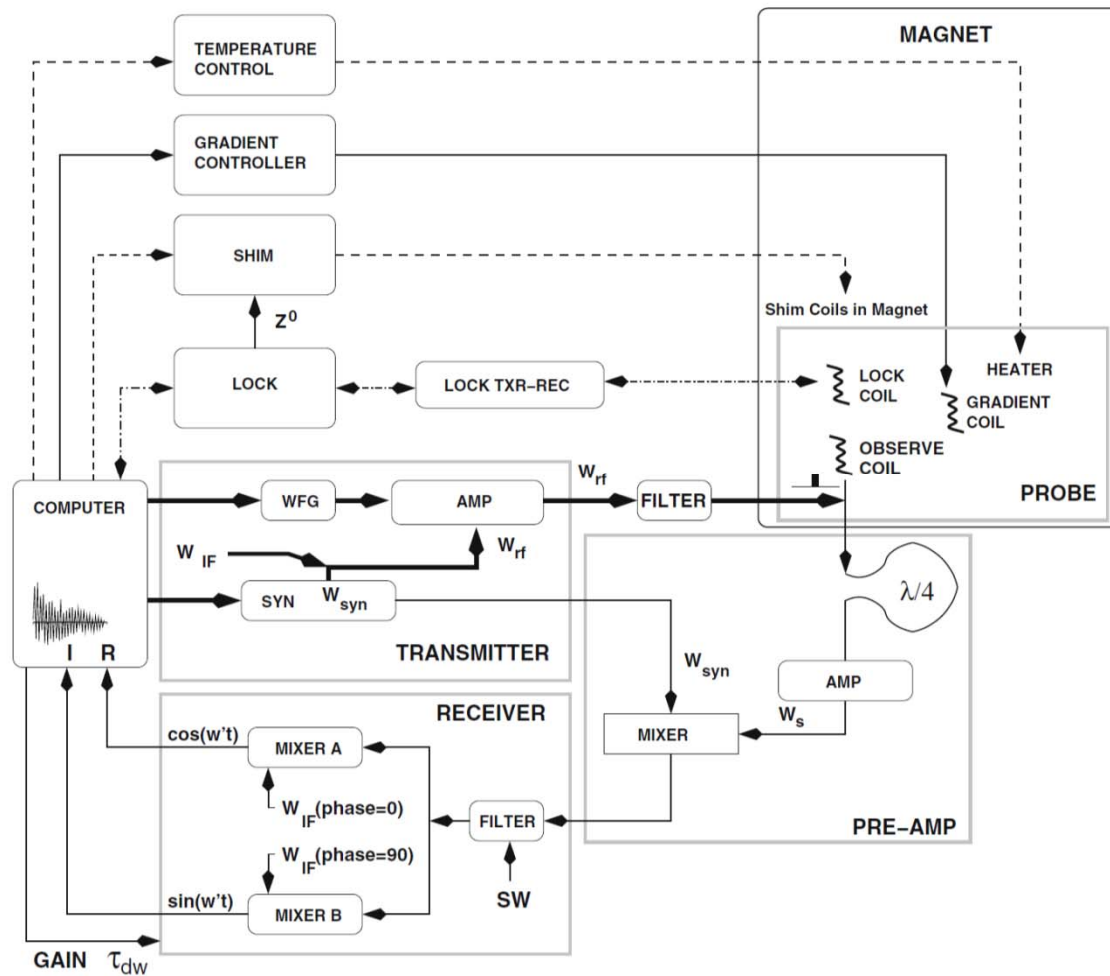


# NMR Instrumentation



From *Protein NMR Spectroscopy*  
Cavanagh *et al.*, Chapt. 3, p. 116

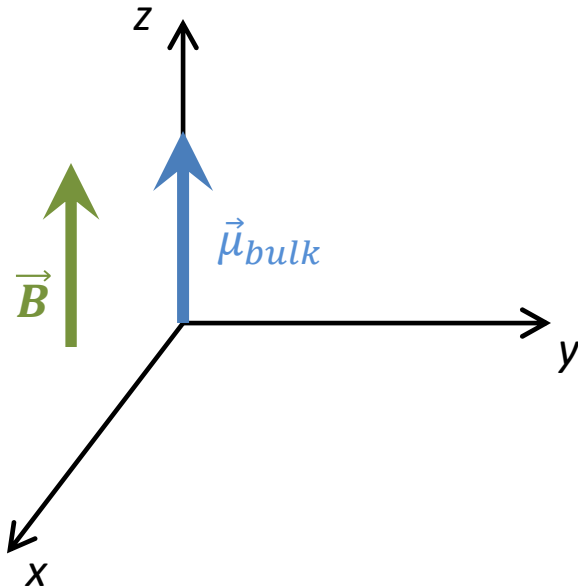
# Block Diagram



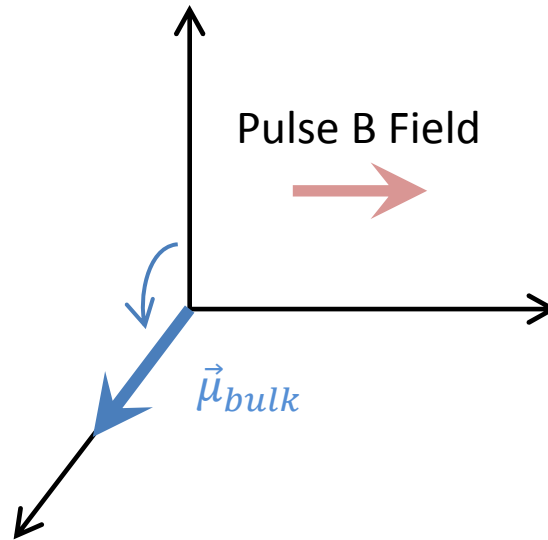
From *Fundamentals of Protein NMR Spectroscopy*  
 Rule & Hitchens, Chapt. 2, p. 30

# 1-Dimensional Pulse Program

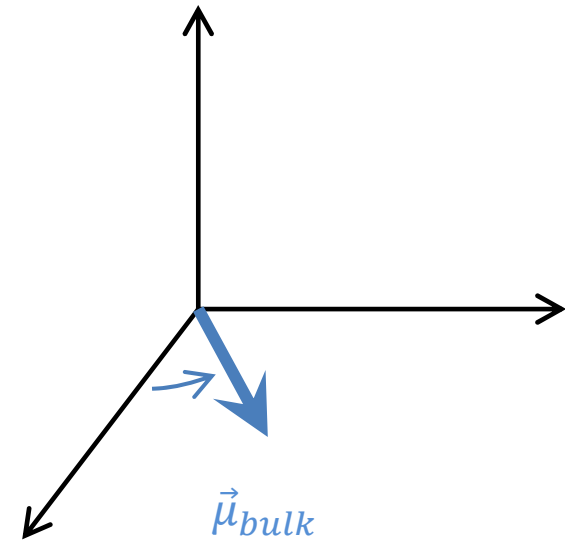
(assumes off-resonance spin in a rotating x, y, z frame)



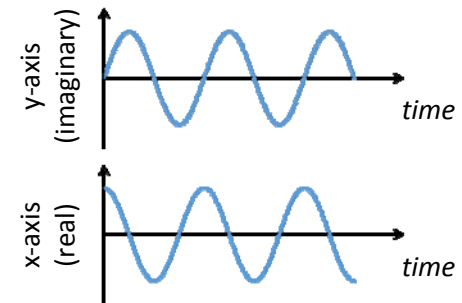
x, y components in a bulk system average out, so bulk magnetization points along z.



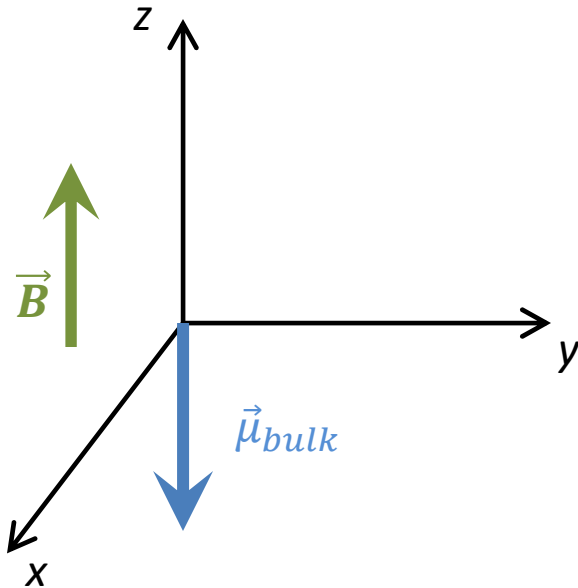
90° pulse along y rotates bulk magnetization to x axis



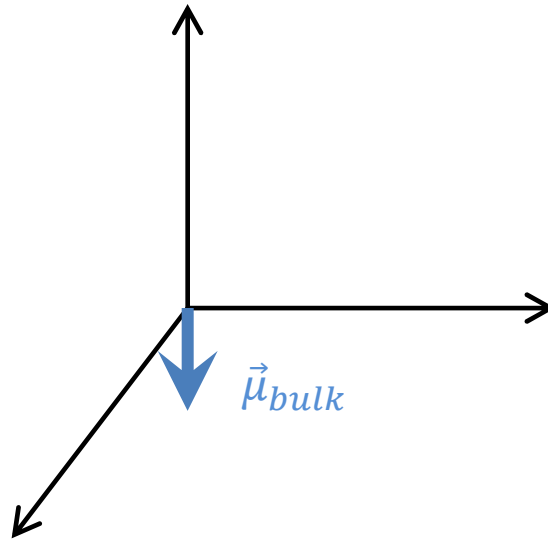
Bulk magnetization precesses in xy plane



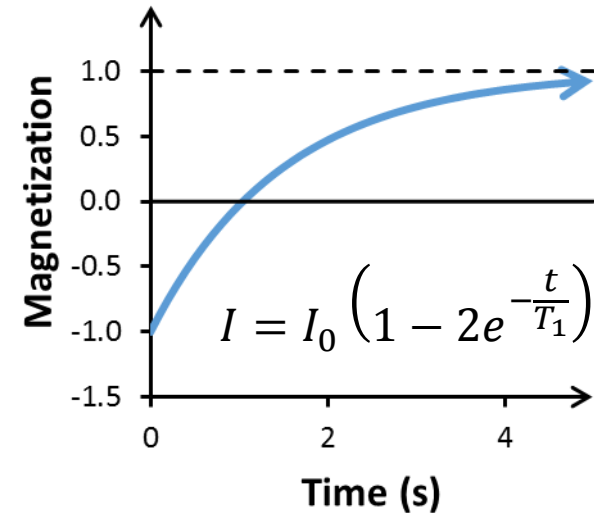
# Relaxation: T1 Relaxation



After a  $180^\circ$  pulse, bulk magnetization points along  $-z$ , but it is not at equilibrium



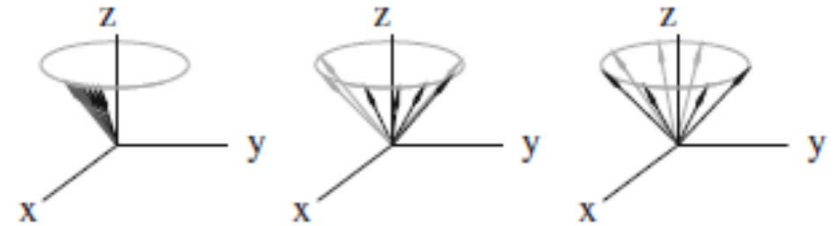
Over time, bulk magnetization returns to  $+z$  axis (equilibrium)



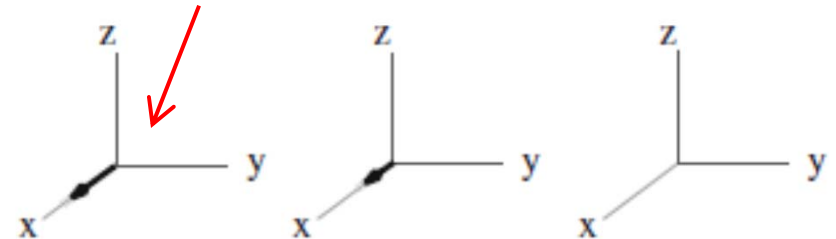
Relaxation with exponential time constant  $T_1$

# Relaxation: T2 Relaxation

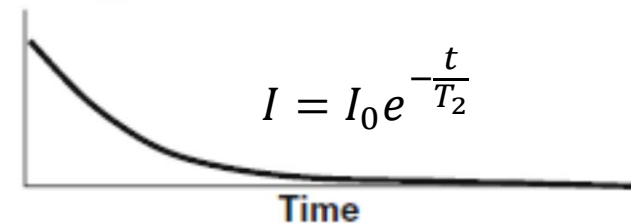
- Bulk magnetization is sum of many individual magnetic dipoles
- Over time dipoles “diphase” – they become randomized
- Once de-phased, there is no net signal to measure



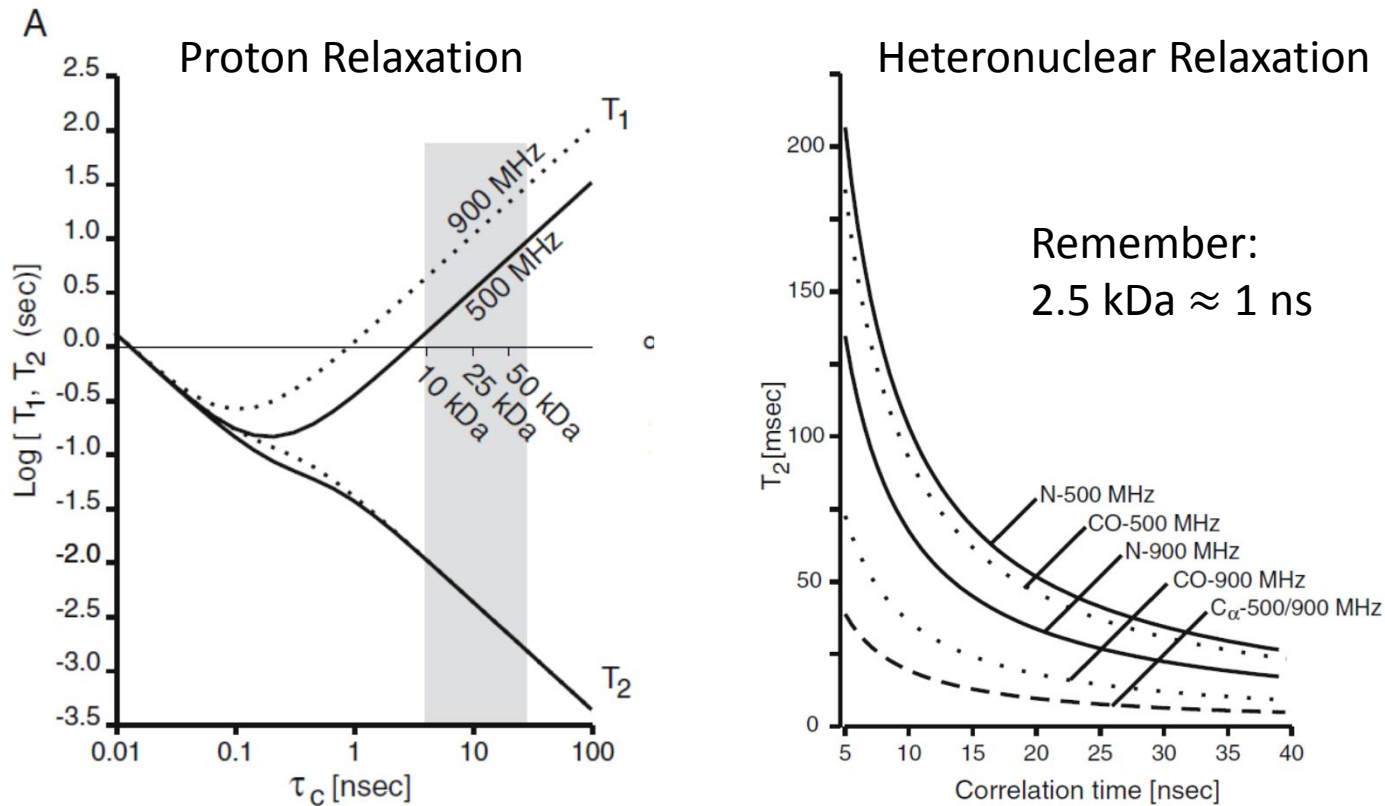
**Note:** On-resonance magnetization rotates at the same rate as the rotating xyz frame; therefore, it appears static.



Observed Signal



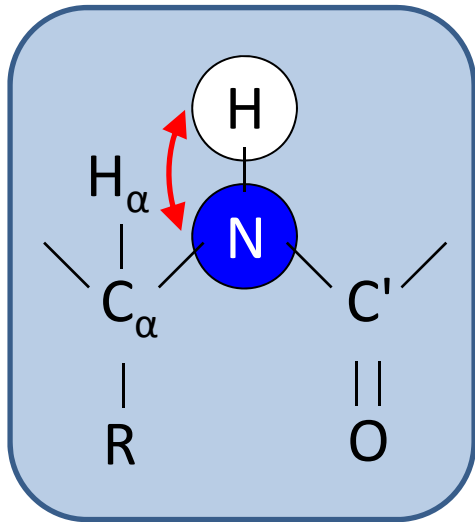
# Relaxation for Proteins



- Big proteins have faster  $T_2$  values



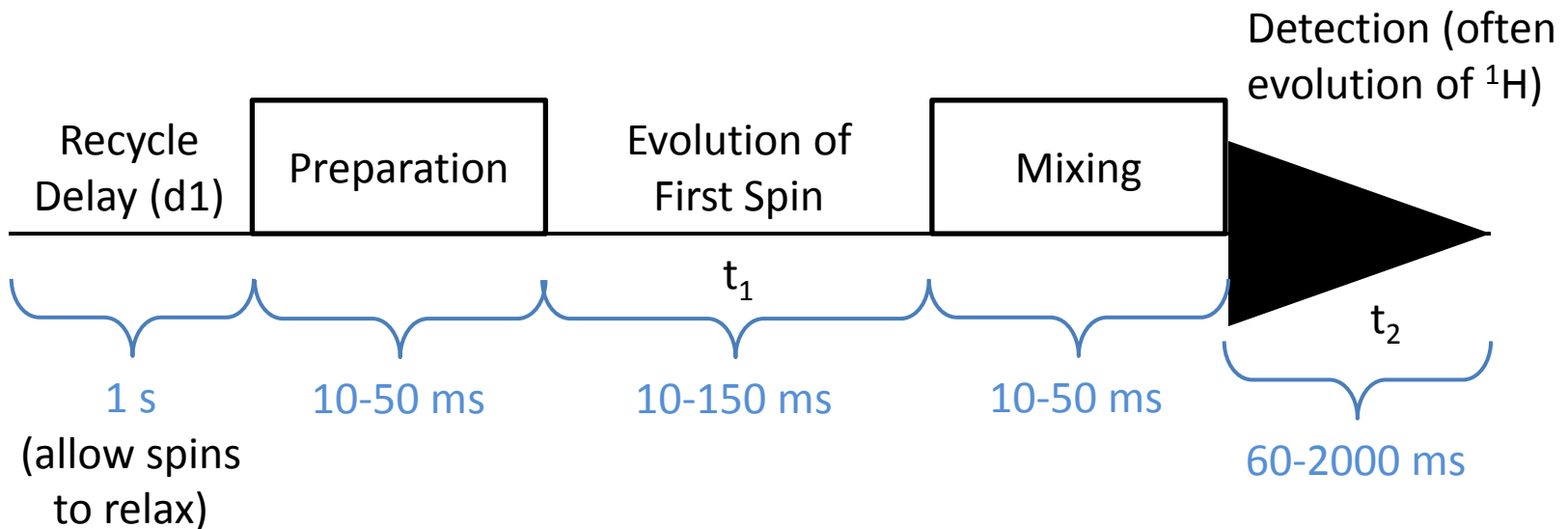
# Multidimensional NMR



**Idea:** Correlate spins through magnetization transfer. This relies on quantum mechanics (and is beyond the scope of this class)

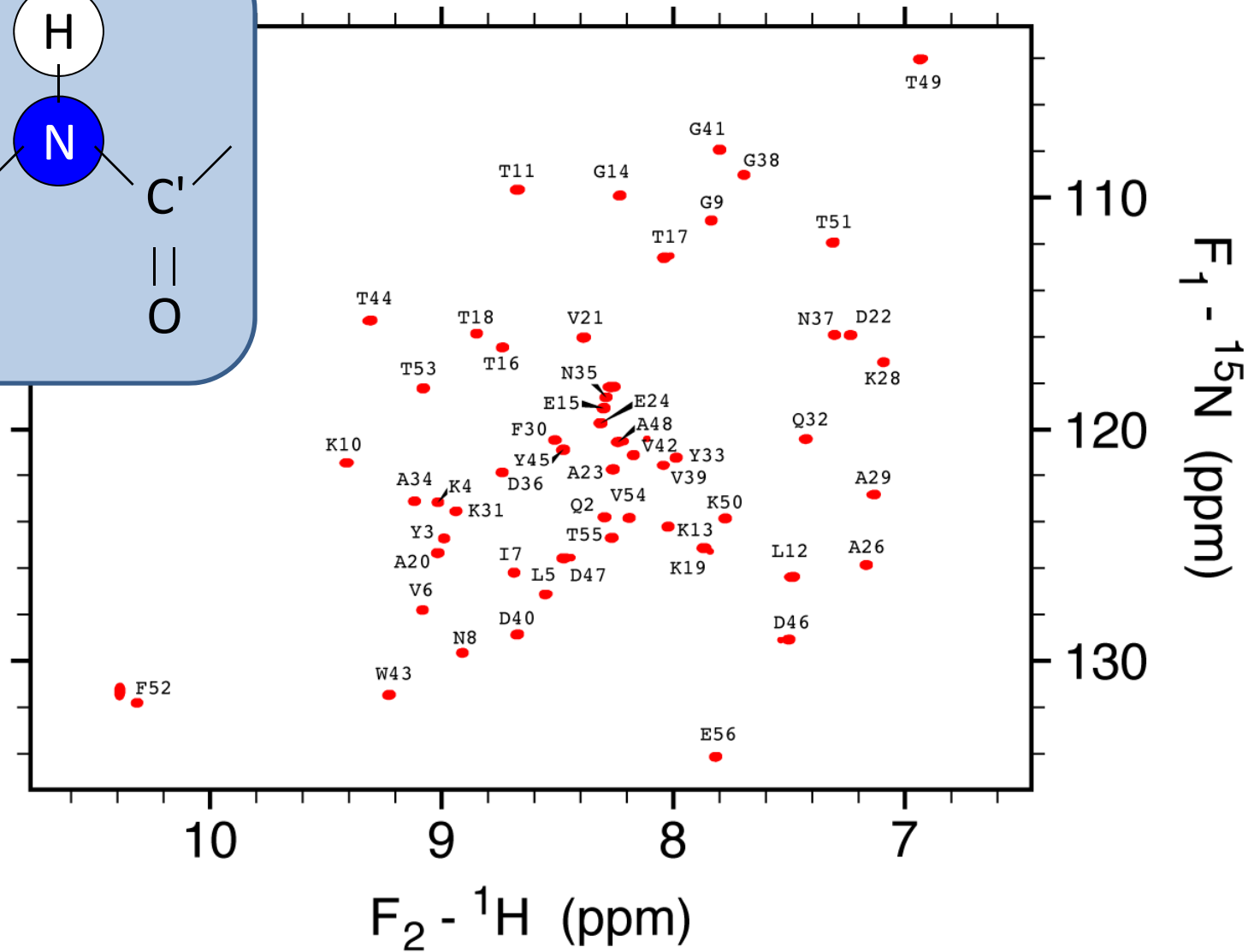
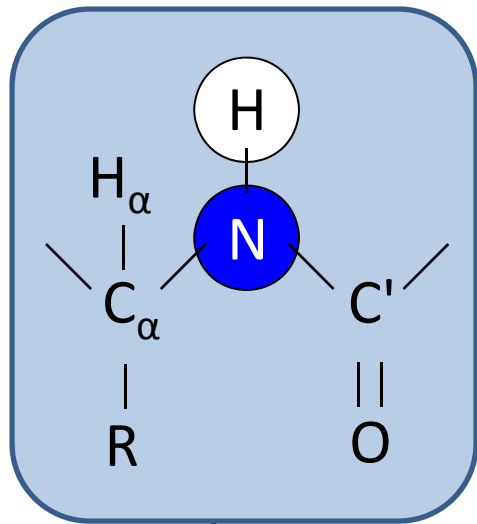
- Start magnetization on nucleus A and evolve chemical shift (a)
- Transfer magnetization to nucleus B and evolve chemical shift (b)
- Plot a peak at coordinates (a, b) corresponding to spin system

# Multidimensional NMR Experiment

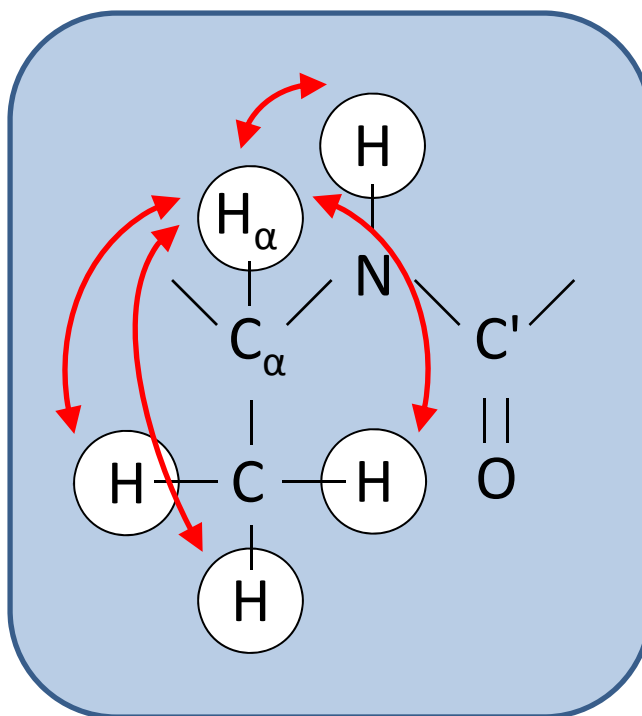


- Multiple evolution/mixing times may be included (3D, 4D experiments)
- **Consideration:** Relaxation times

# 2D NMR $^{15}\text{N}$ HSQC: GB3

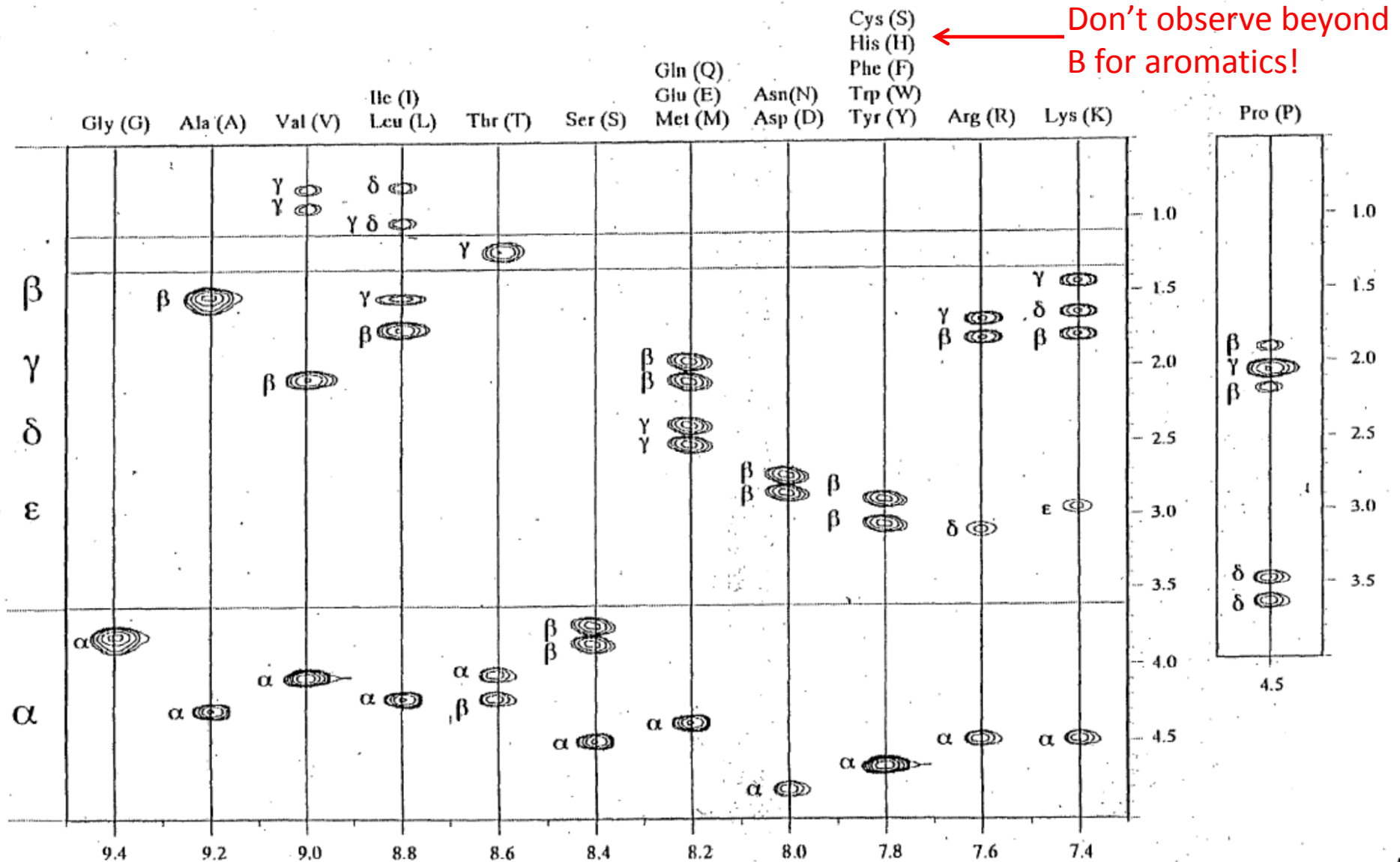


# $^1\text{H}$ TOCSY

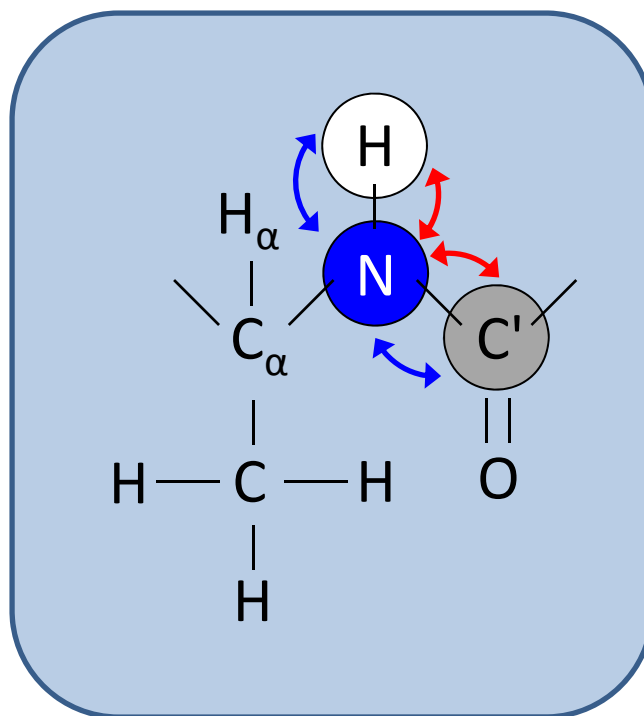


- Magnetization “hops” from nucleus to nucleus
- Example: Crosspeaks observed between H<sub>N</sub> and: H<sub>α</sub>, H<sub>β</sub>, H<sub>γ</sub> (gets weaker for more hops)

# $^1\text{H}$ TOCSY Fingerprints



# 3D HNCO

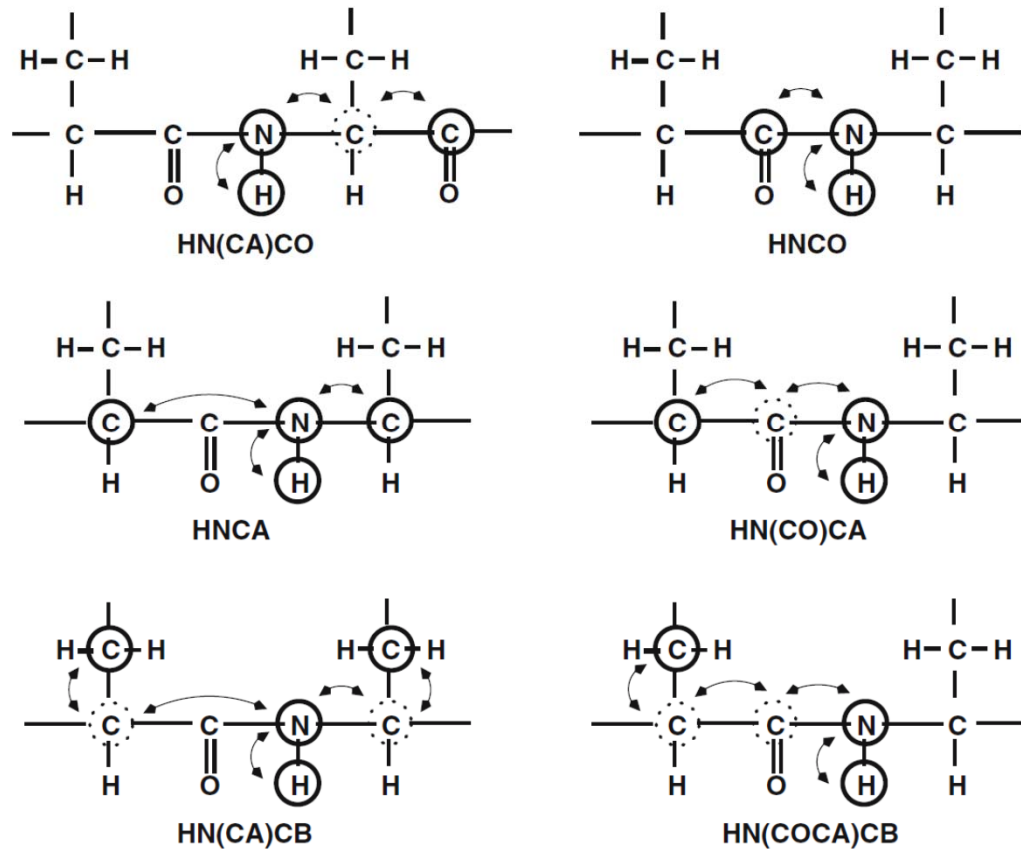


**Out:** Red transfers occur during preparation period

**Back:** Blue transfers occur between chemical shift labeling steps on the way back

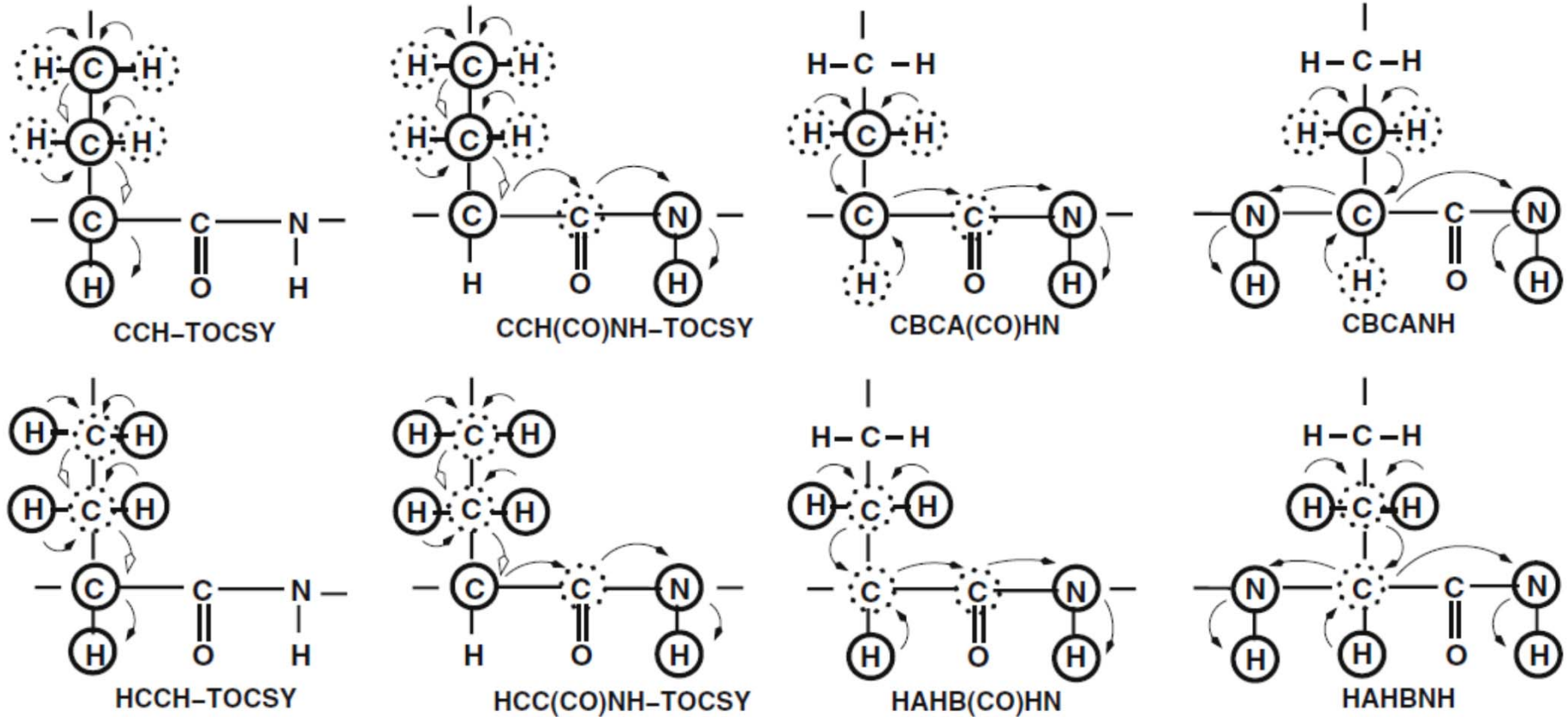
- See peaks at  $H_N$ , N, and  $C'_{i-1}$  (i.e. the C' of the prior residue)
- Requires  $^{13}\text{C}$  and  $^{15}\text{N}$  labeled protein

# Backbone Assignment



From *Fundamentals of Protein NMR Spectroscopy*  
Rule & Hitchens, Chapt. 14, p. 281

# Sidechain Assignment





# Summary

- NMR spectra are Fourier transforms of time domain signals (FIDs)
- In a magnetic field, individual spins feel a torque, and  $\frac{d\vec{\mu}}{dt} = \gamma\vec{\mu} \times \vec{B}$
- The frequency of absorption ( $\omega = \gamma B_0$ ) is **identical** to the Larmor precession frequency ( $|\Omega| = \gamma B_0$ )
- NMR spins will relax over time
- Magnetization transfer  $\rightarrow$  multidimensional NMR