

Fluorescence Workshop
UMN Physics
June 8-10, 2006

**Fluorescence Microscopy and
Fluorescence Correlation Spectroscopy**
Joachim Mueller



Fluorescence Microscopy

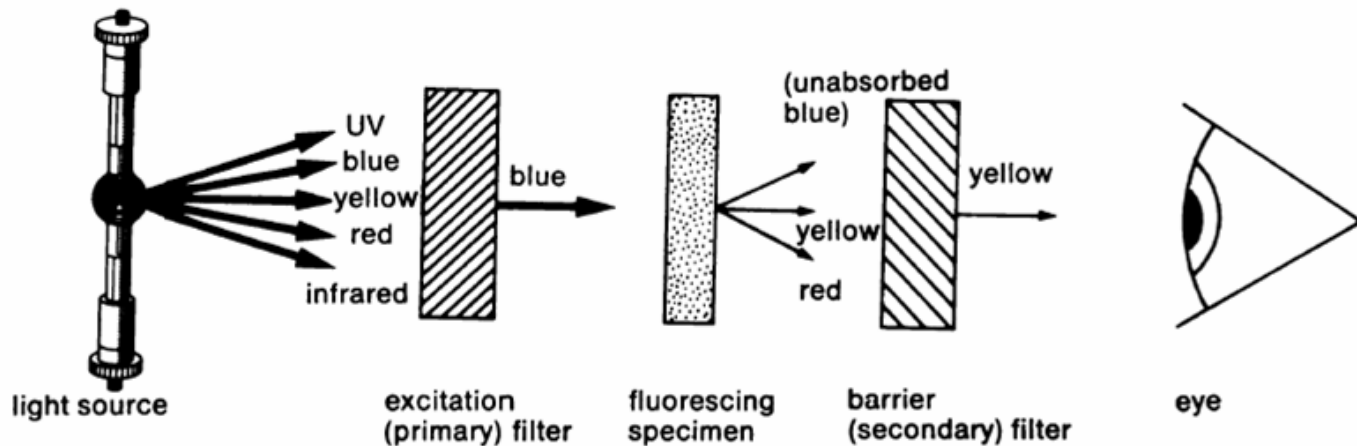
Use a microscope as
a fluorometer



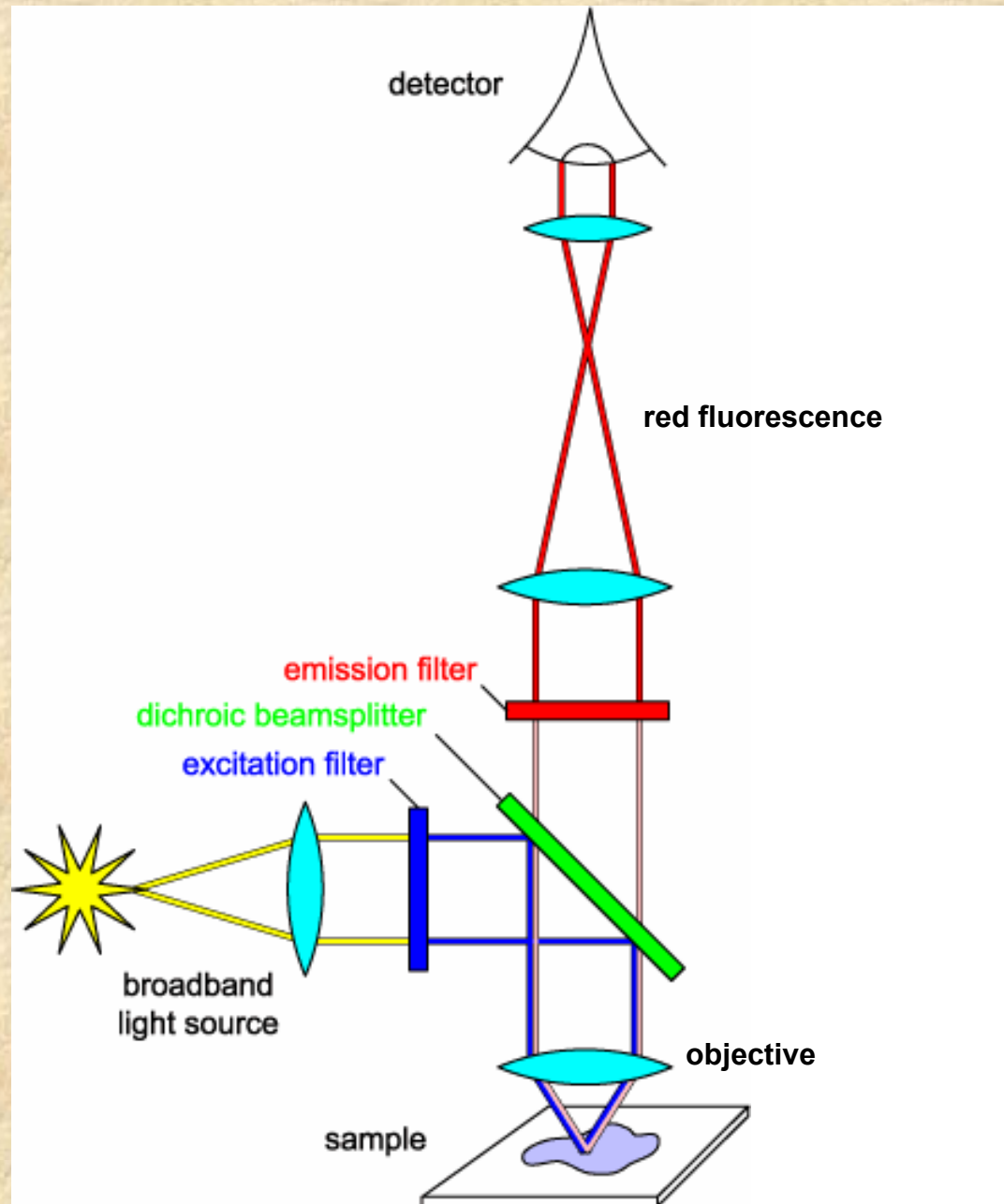
Advantages:

- superb optics
- very high collection efficiency
- imaging
- allows single cell measurements
- single molecule experiments

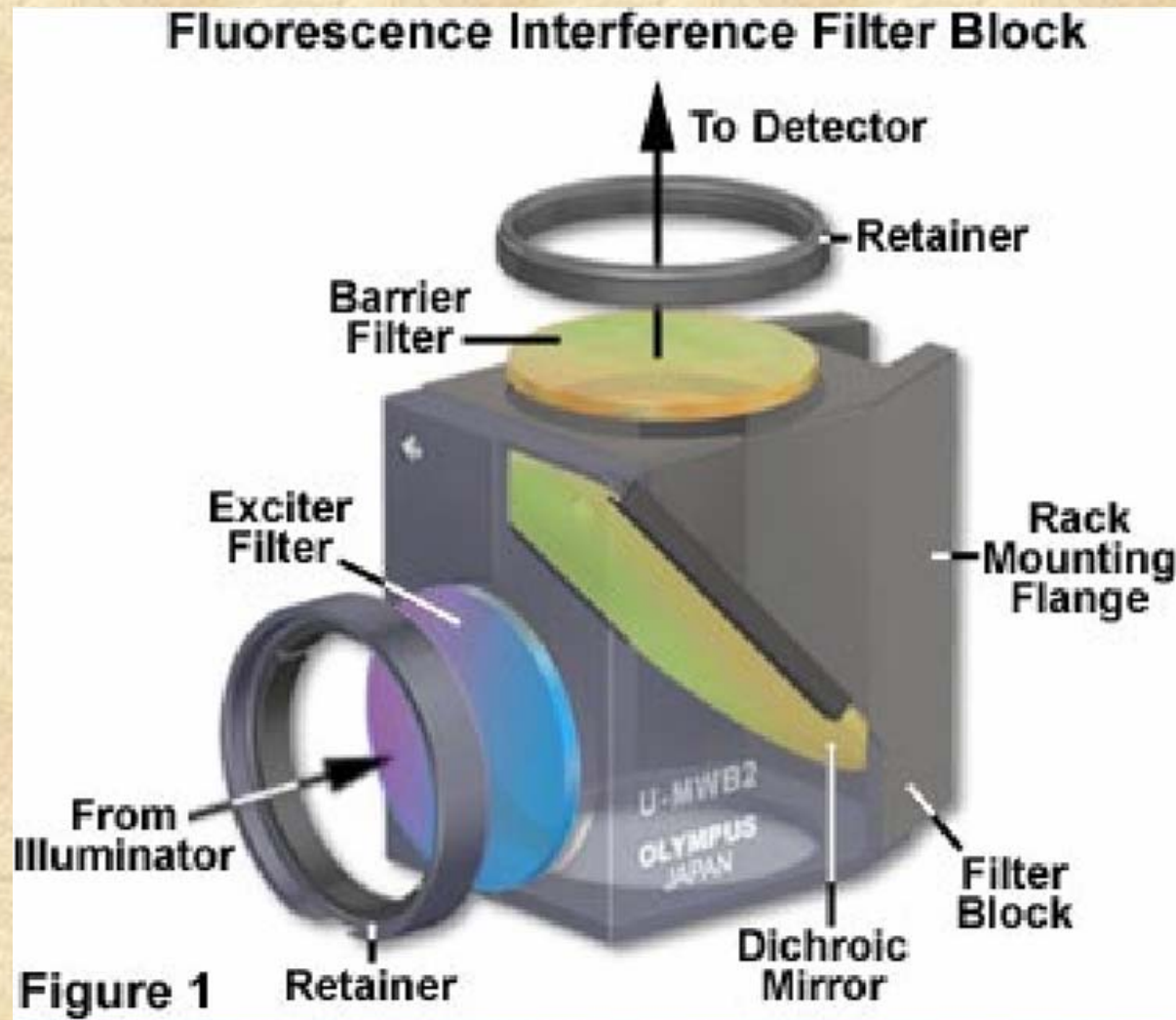
The microscope as a filter fluorometer with focusing optics



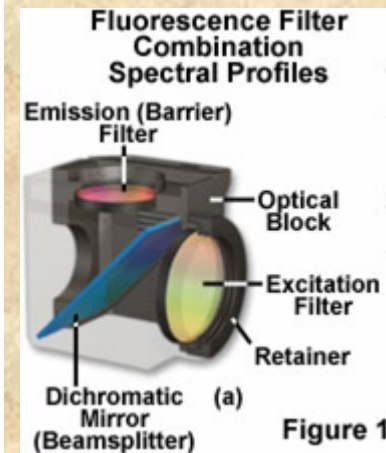
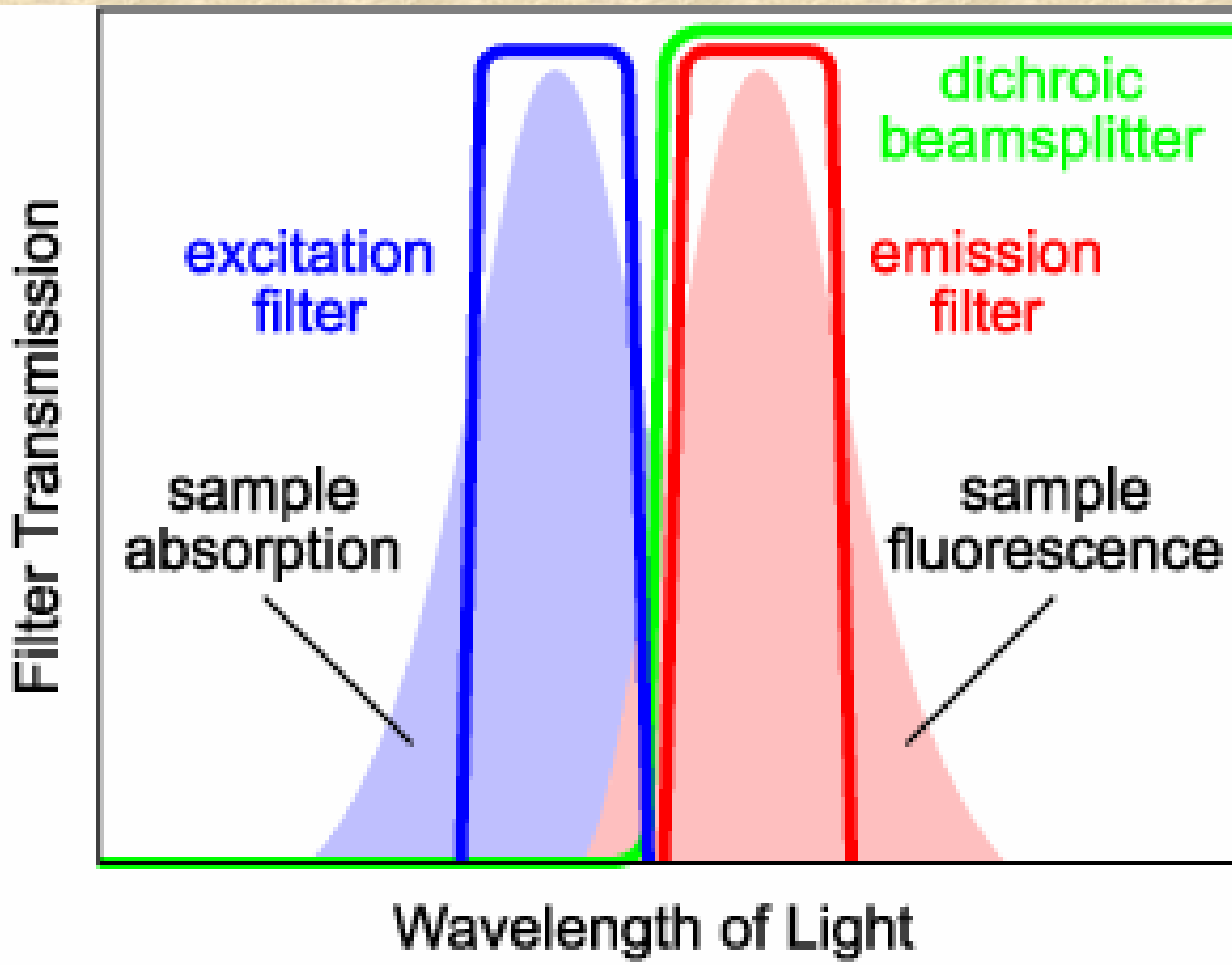
Basic design of a fluorescent microscope



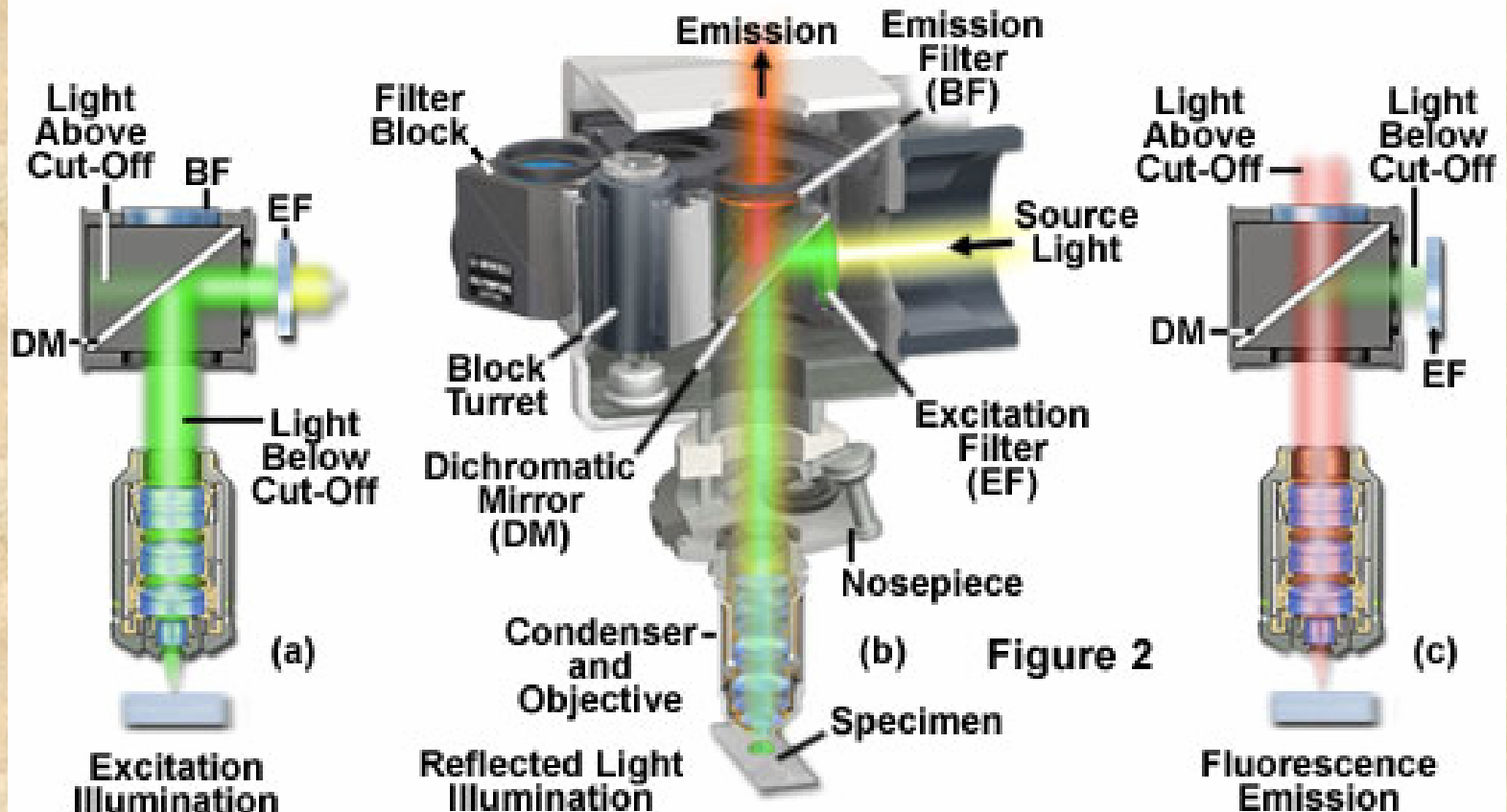
Filters



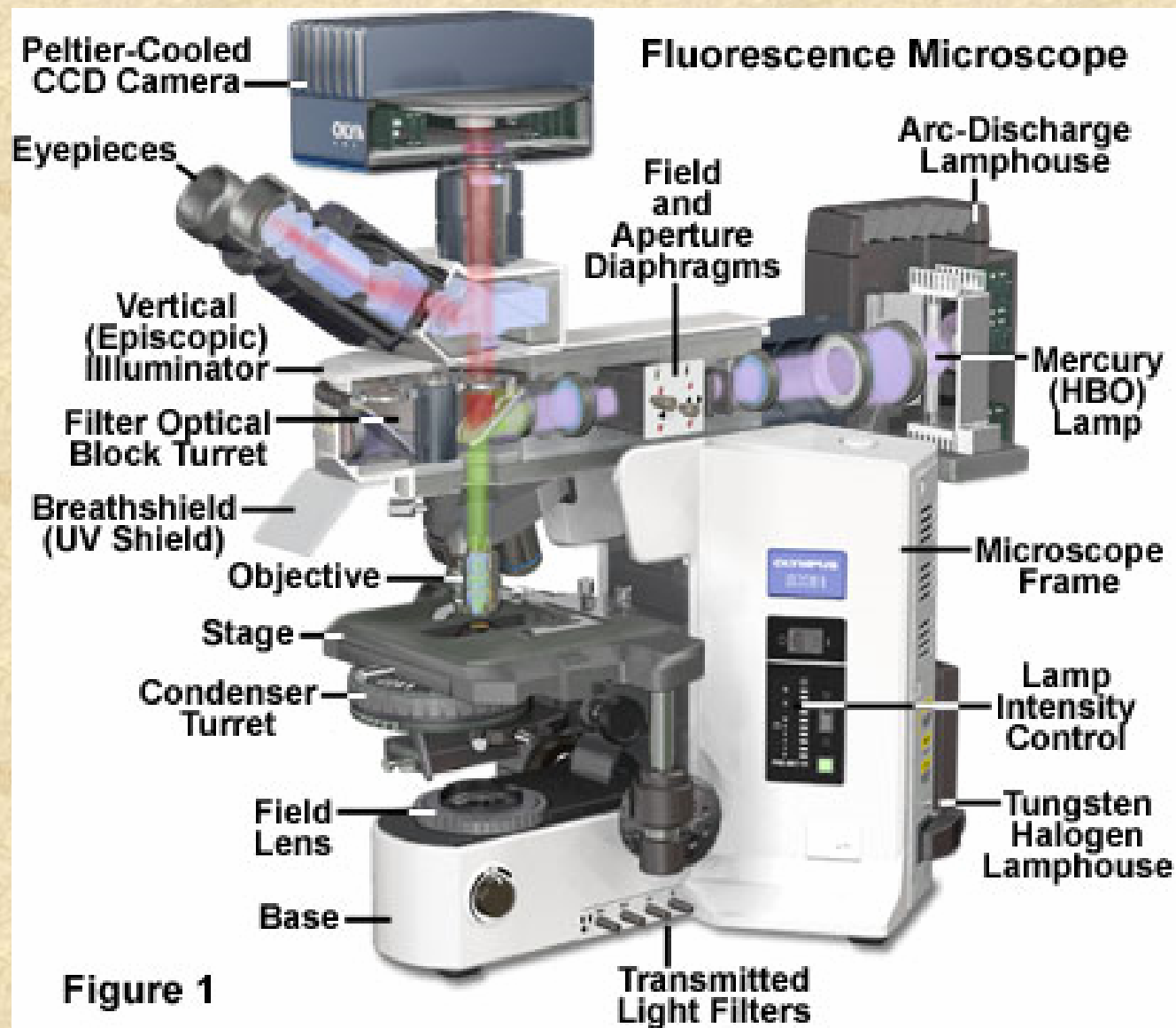
Selecting Filters



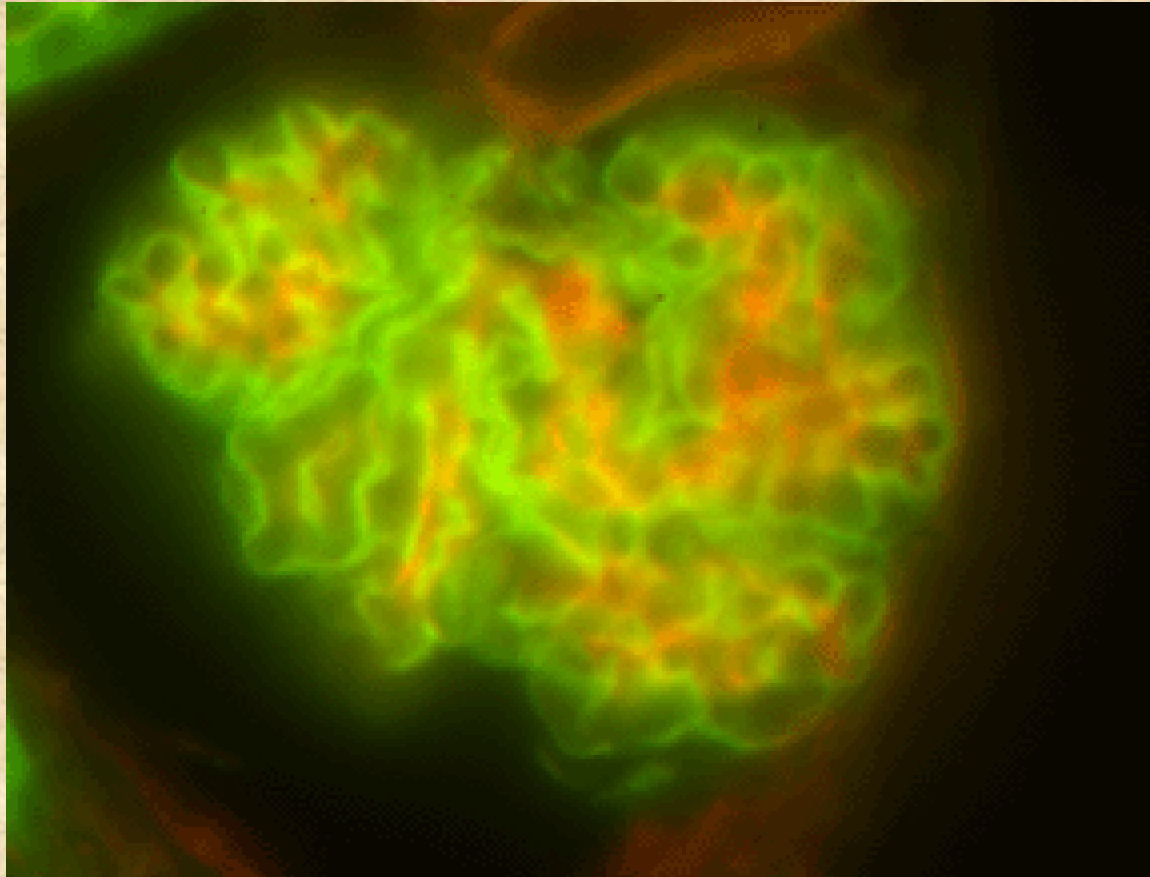
Dichromatic Mirror Function in Reflected Light Fluorescence Illumination



Anatomy of a Fluorescence Microscope



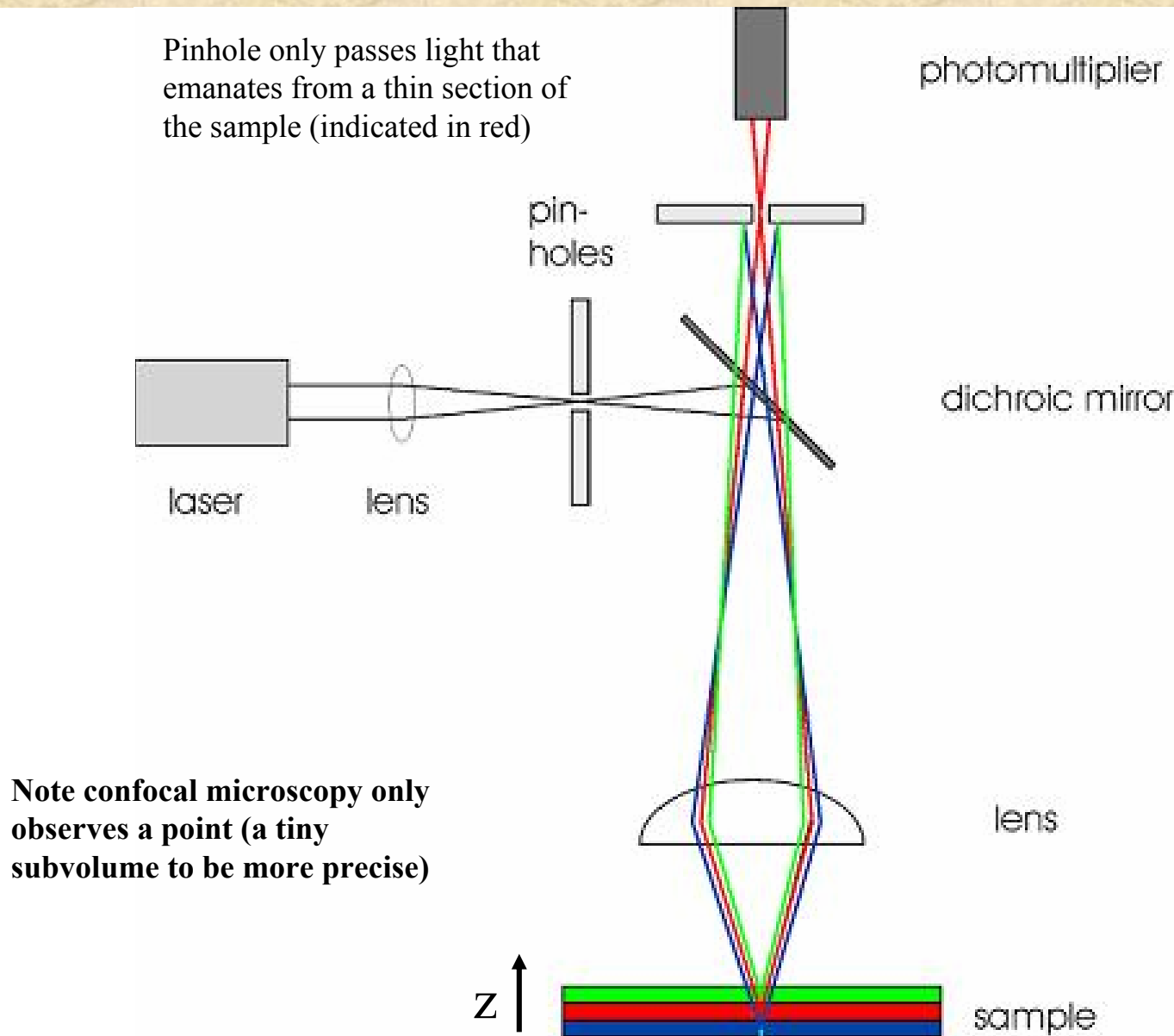
Widefield-fluorescence microscope image



Widefield fluorescence image of a 16 micron thick section of fluorescently-labeled mouse kidney.

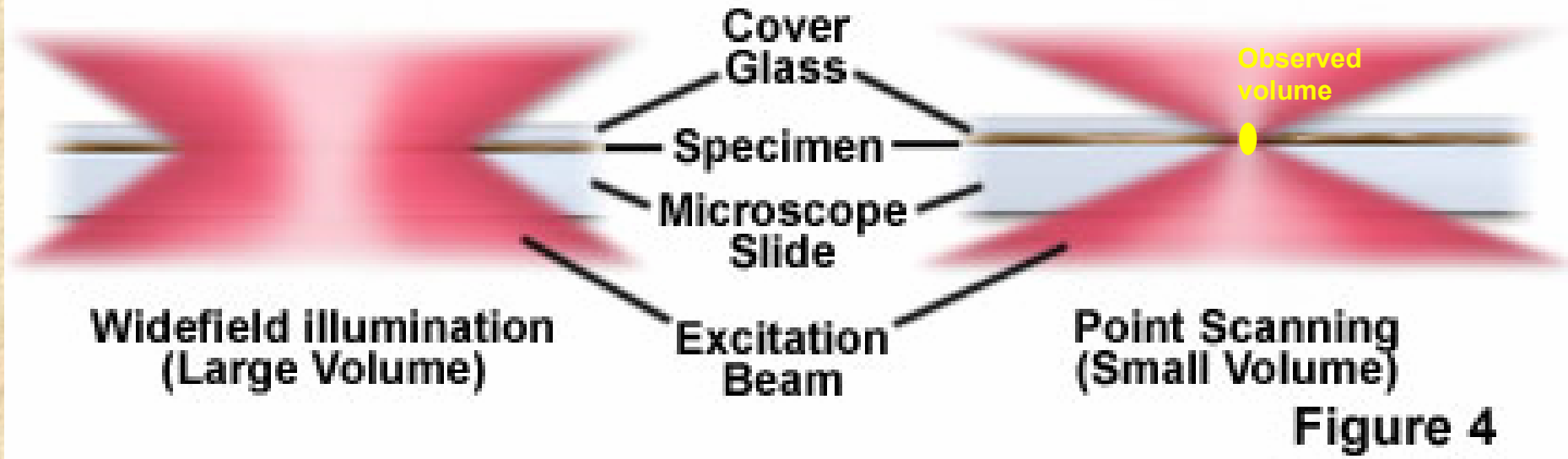
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Principle of Confocal Microscopy

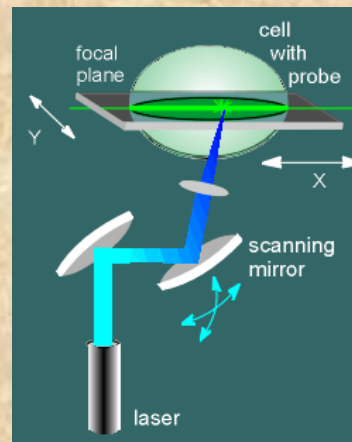
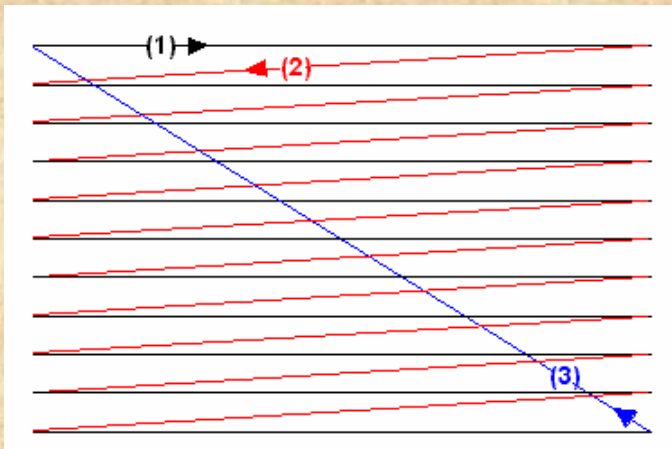


Laser Scanning Confocal Microscopy (LSCM):

Widefield versus Confocal Point Scanning of Specimens

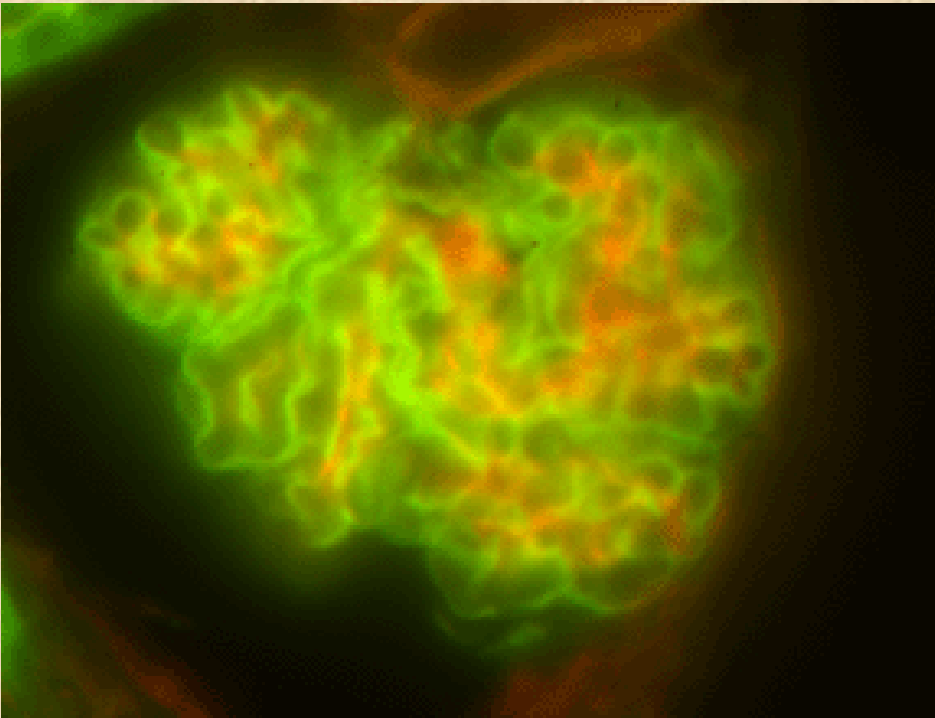


Need to perform a **raster scan** to build up an image point by point



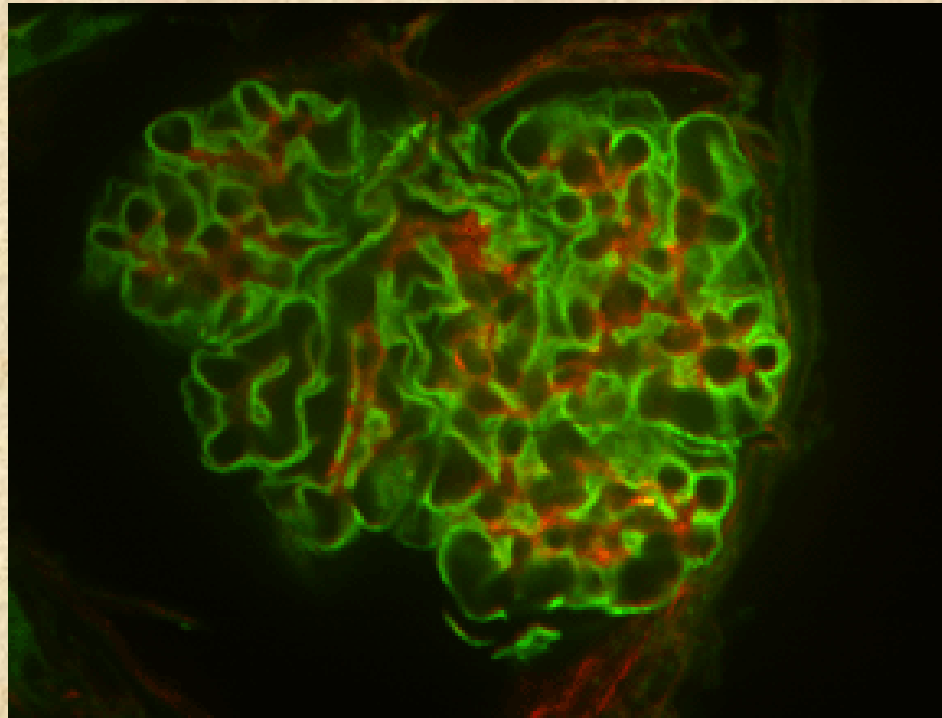
Two electronically driven scan mirrors move the laser spot on the sample in a raster-like fashion.

Widefield Image



Widefield fluorescence image of a 16 micron thick section of fluorescently-labeled mouse kidney.

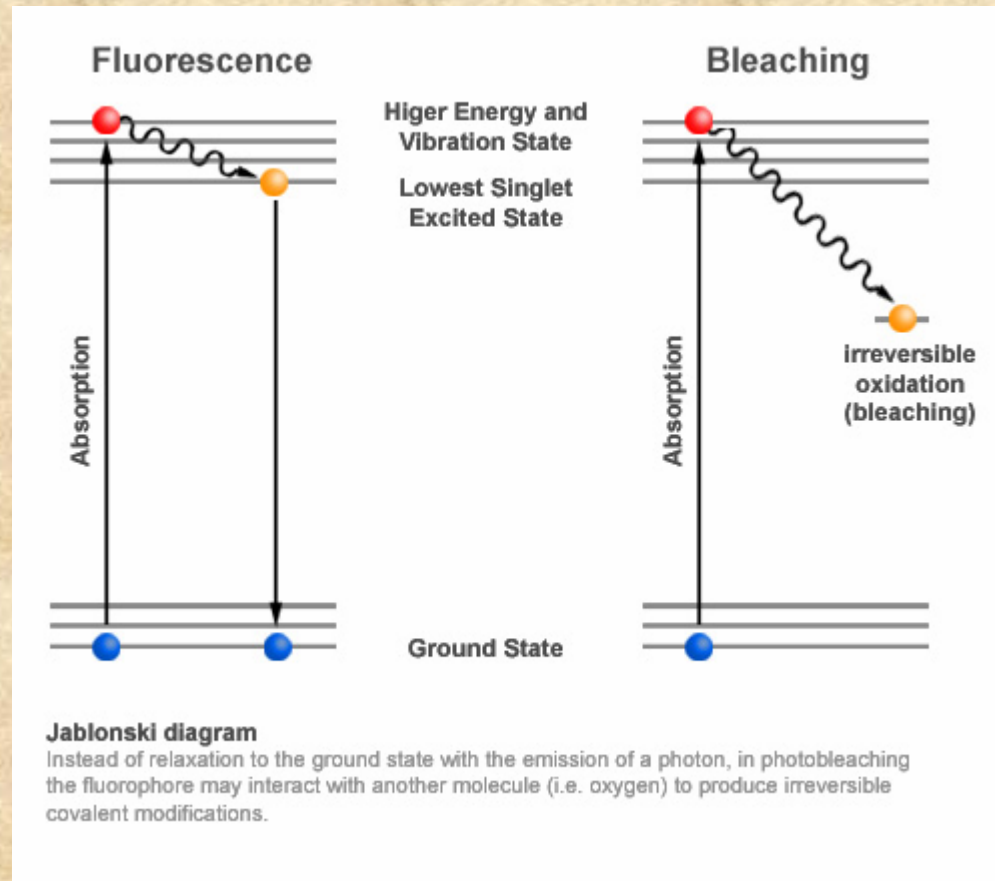
Confocal Image



The same specimen shown on the left, taken with a confocal microscope.

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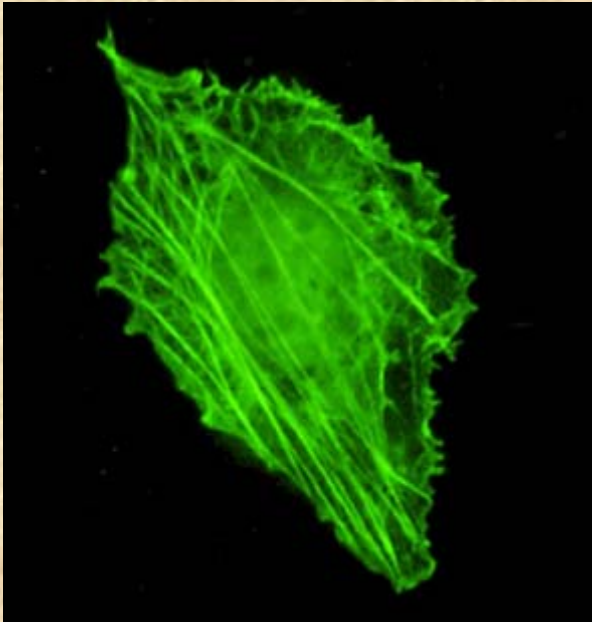
Photobleaching



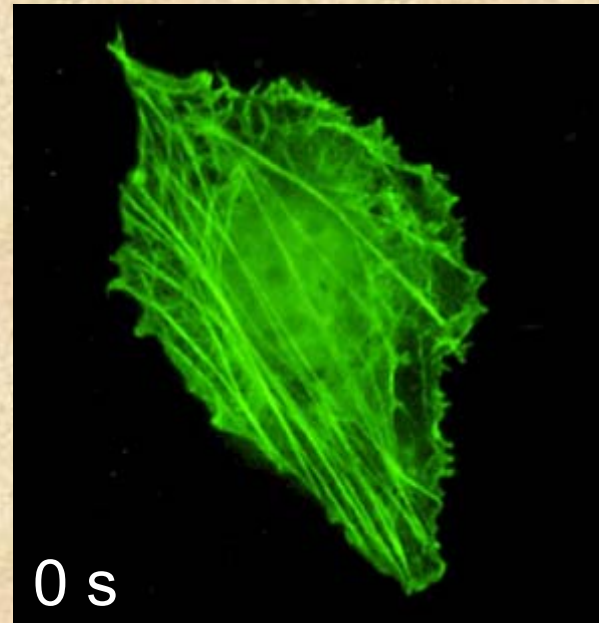
The average number of excitation and emission cycles that occur for a particular fluorophore before photobleaching is dependent upon the molecular structure and the local environment. Some fluorophores bleach quickly after emitting only a few photons, while others that are more robust can undergo thousands or millions of cycles before bleaching.

Photobleaching

original image

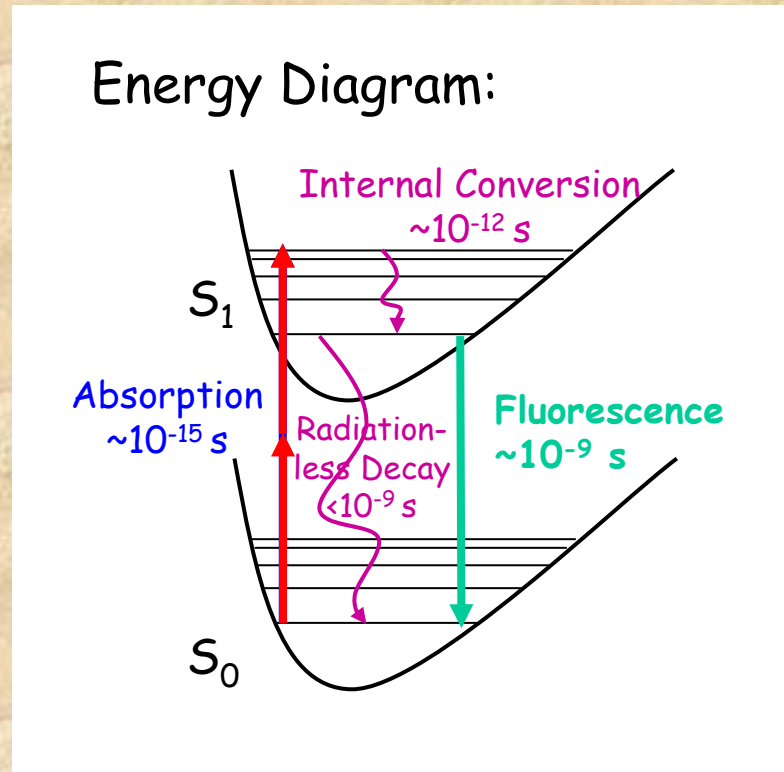


Photobleached image



Two-Photon Microscopy: Principle

Now consider two-photon absorption



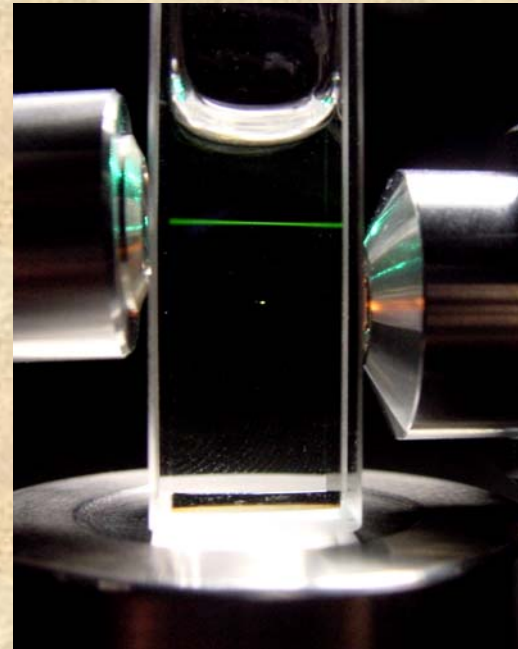
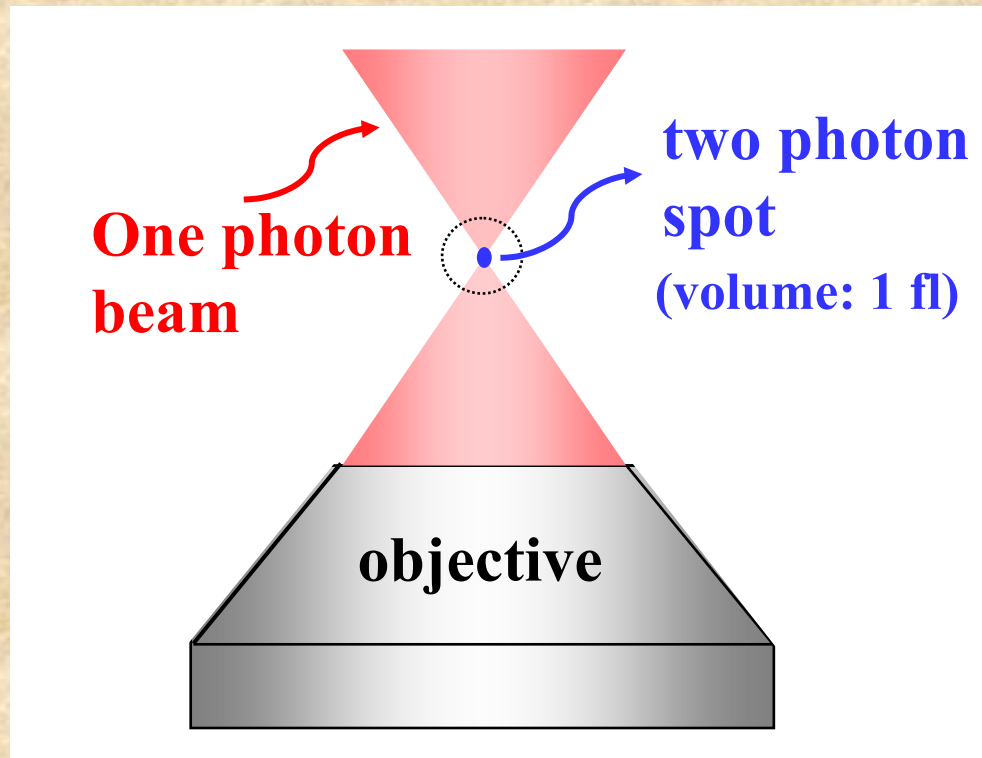
Two-photon absorption is an optical nonlinear process

Two-Photon Fluorescence

Simultaneous absorption of two-photons is a rare process:

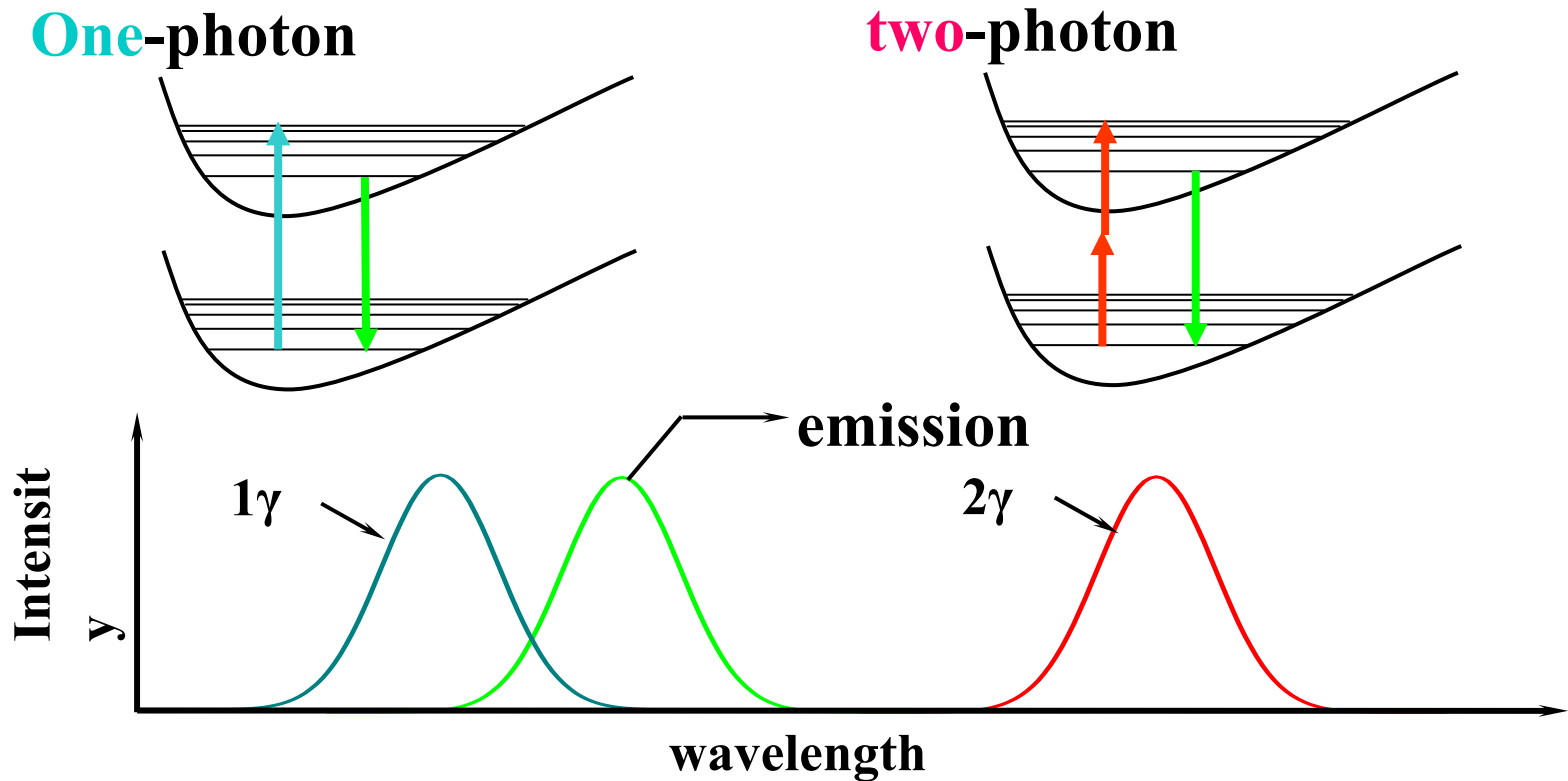
Maximize two-photon effect by increasing the photon flux

- **spatially** by focusing the light
- **temporally** (ultrafast laser pulses)



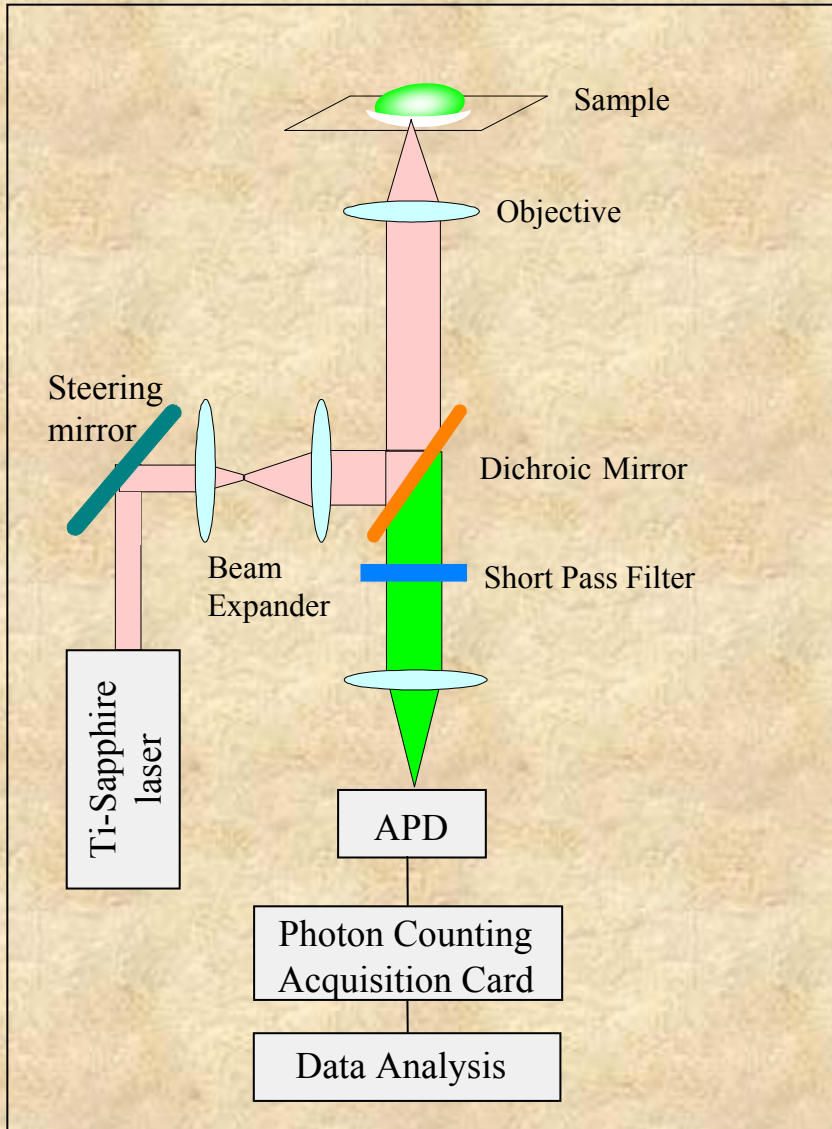
Inherent 3 - dimensional optical sectioning effect!

Two-photon spectroscopy

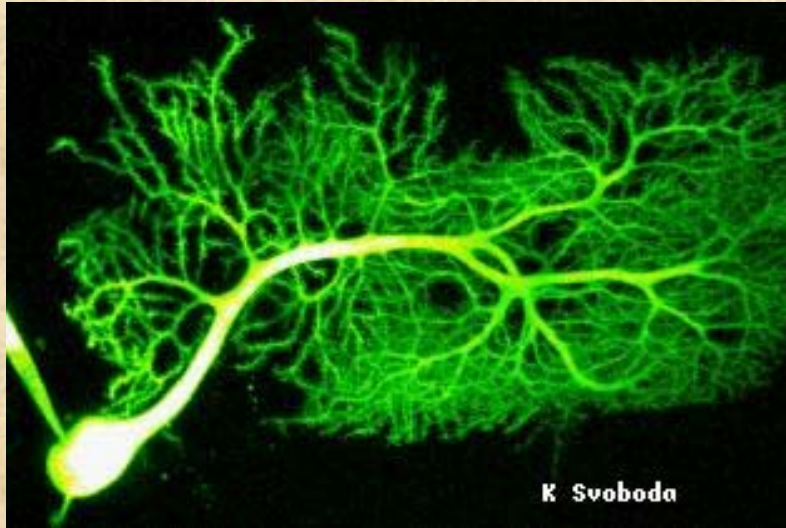


Two-photon absorption is spectrally well separated from the fluorescence! Note that Raman of the solvent will not occur within the fluorescence emission spectrum.

Two-photon Instrumentation



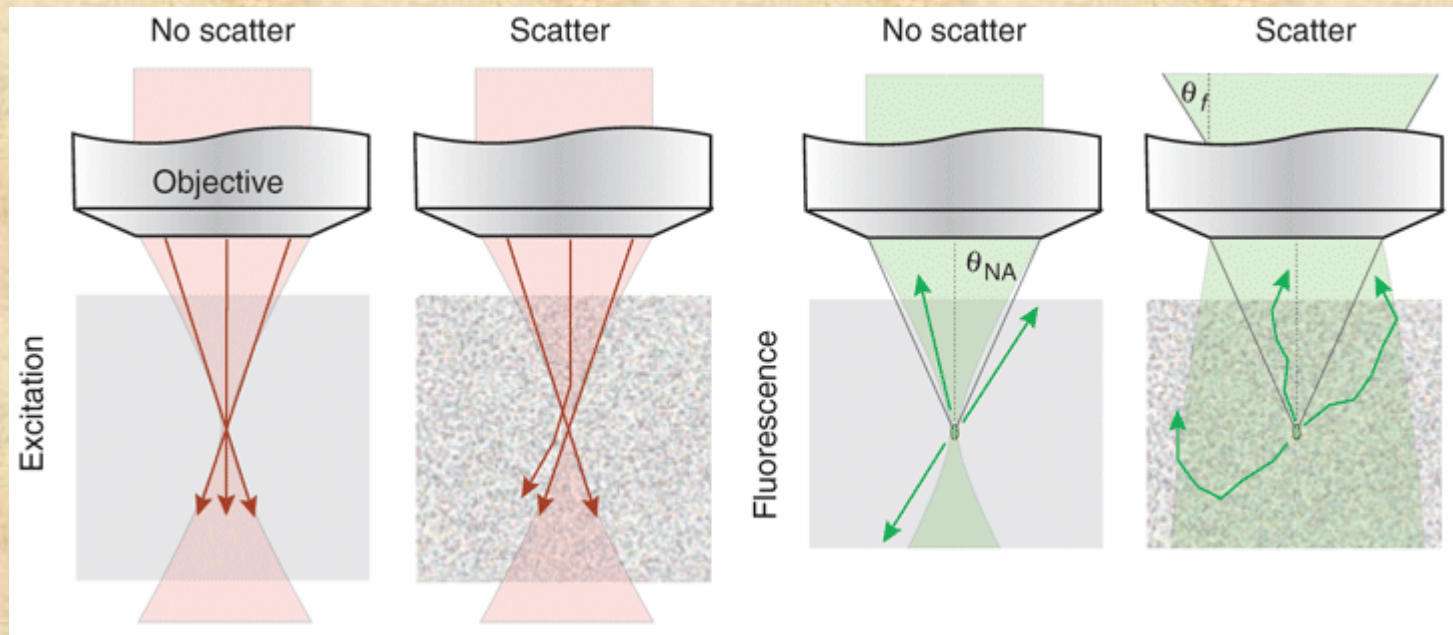
Two-photon Imaging



Purkinje neurone in a living brain slice filled with fluorescein dextran imaged with two-photon excitation laser scanning microscopy (Svoboda, Cold spring Harbor Laboratories)

Two-photon image resolution is essentially the same as that of confocal microscopy. However, imaging in the presence of significant scatter (such as in thick tissue) requires two-photon excitation.

Also note that photobleaching in two-photon microscopy is strictly restricted to the excitation volume!



Fluorescence Fluctuation Spectroscopy

Q: How many fluorescent molecules are (on average) in the two-photon (or confocal) volume of the microscope?

A: That depends on the concentration. At a high concentration there are more molecules in the volume than at low concentrations.

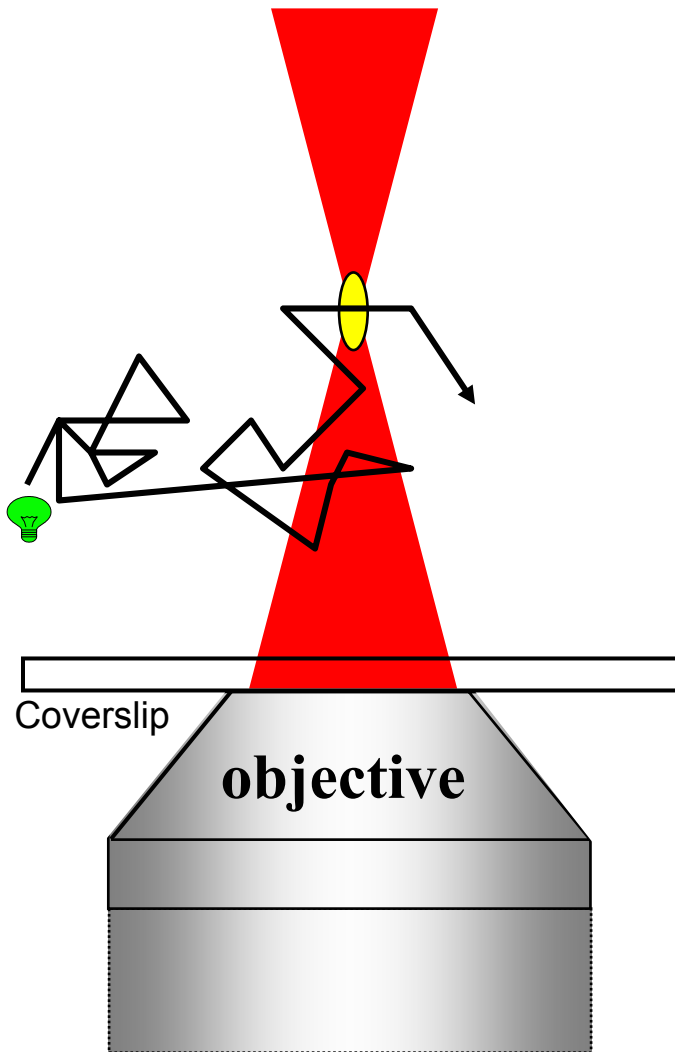
Q: Ok, many proteins in cells have nanomolar concentrations. How many proteins (assuming $c = 1 \text{ nM}$) are now in the volume?

A: Let me calculate ... (Volume is 1 femtoliter, Avogadro's number is 6×10^{23} , $c = 1 \text{ nM}$). The number I get is a **single molecule** per observation volume. Well that's ok, fluorescence is very sensitive and can detect single molecules.

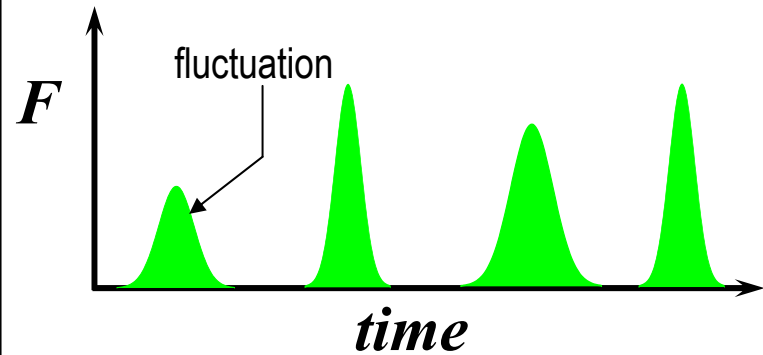
Q: Proteins in a solution (and in a cell) are typically mobile. They diffuse around. What will happen if the single molecule moves around? Also a single molecule is in the volume **on average**. Is there a chance that sometimes there will be two or no molecules in the volume?

A: Yes, the number of molecules will **fluctuate** as they diffuse in and out of the observation volume. Because two molecules produce more fluorescence than a single molecule there will be **fluctuations in the fluorescence intensity**.

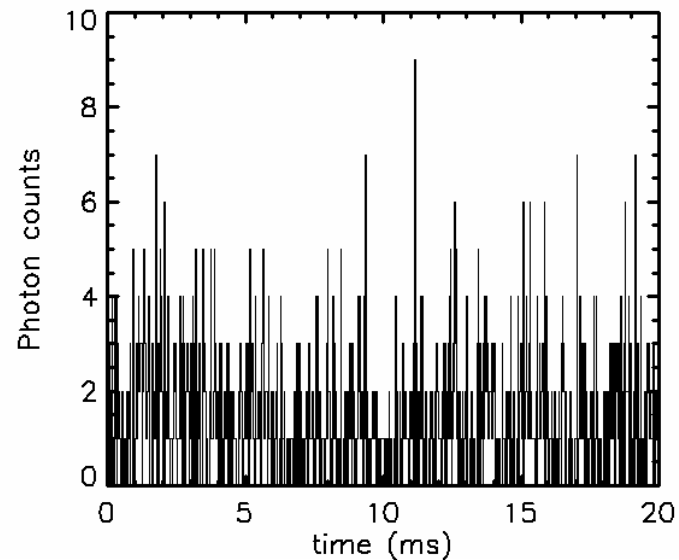
Fluorescence Fluctuation Spectroscopy



Fluorescence intensity:

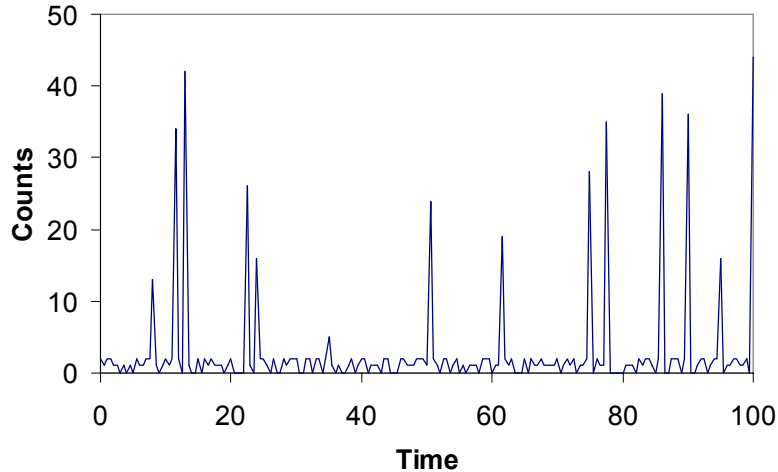


Raw data: Photon Counts

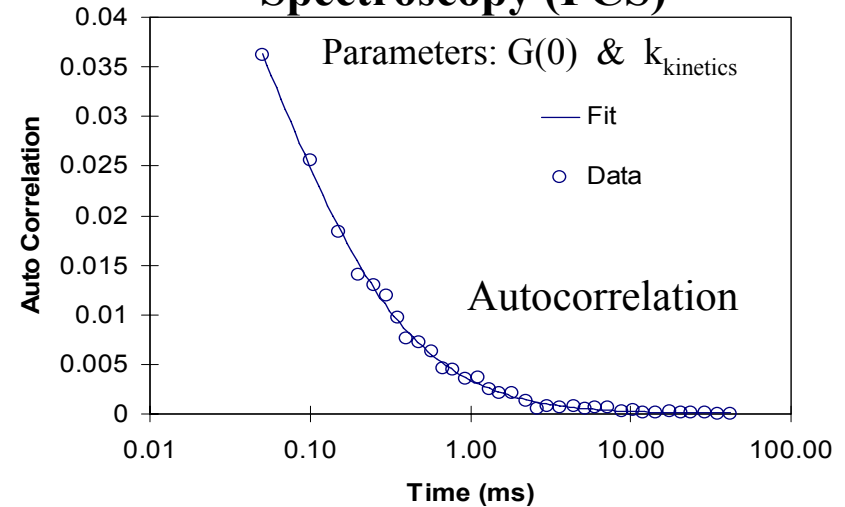


Statistical Analysis of the Fluctuations required

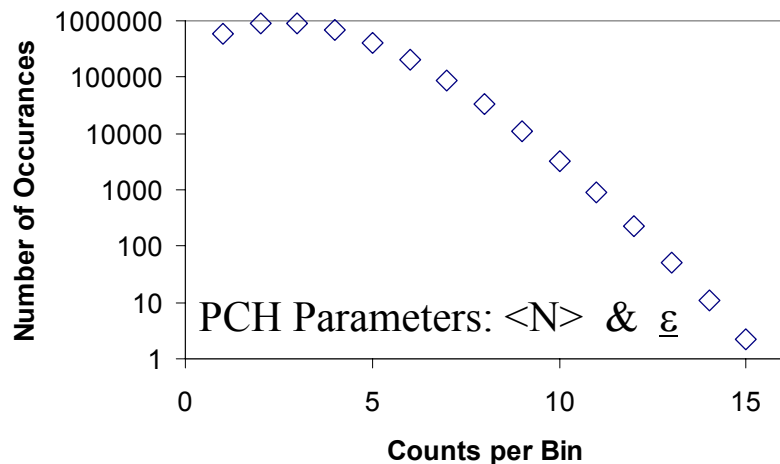
Photon counts



Fluorescence Correlation Spectroscopy (FCS)



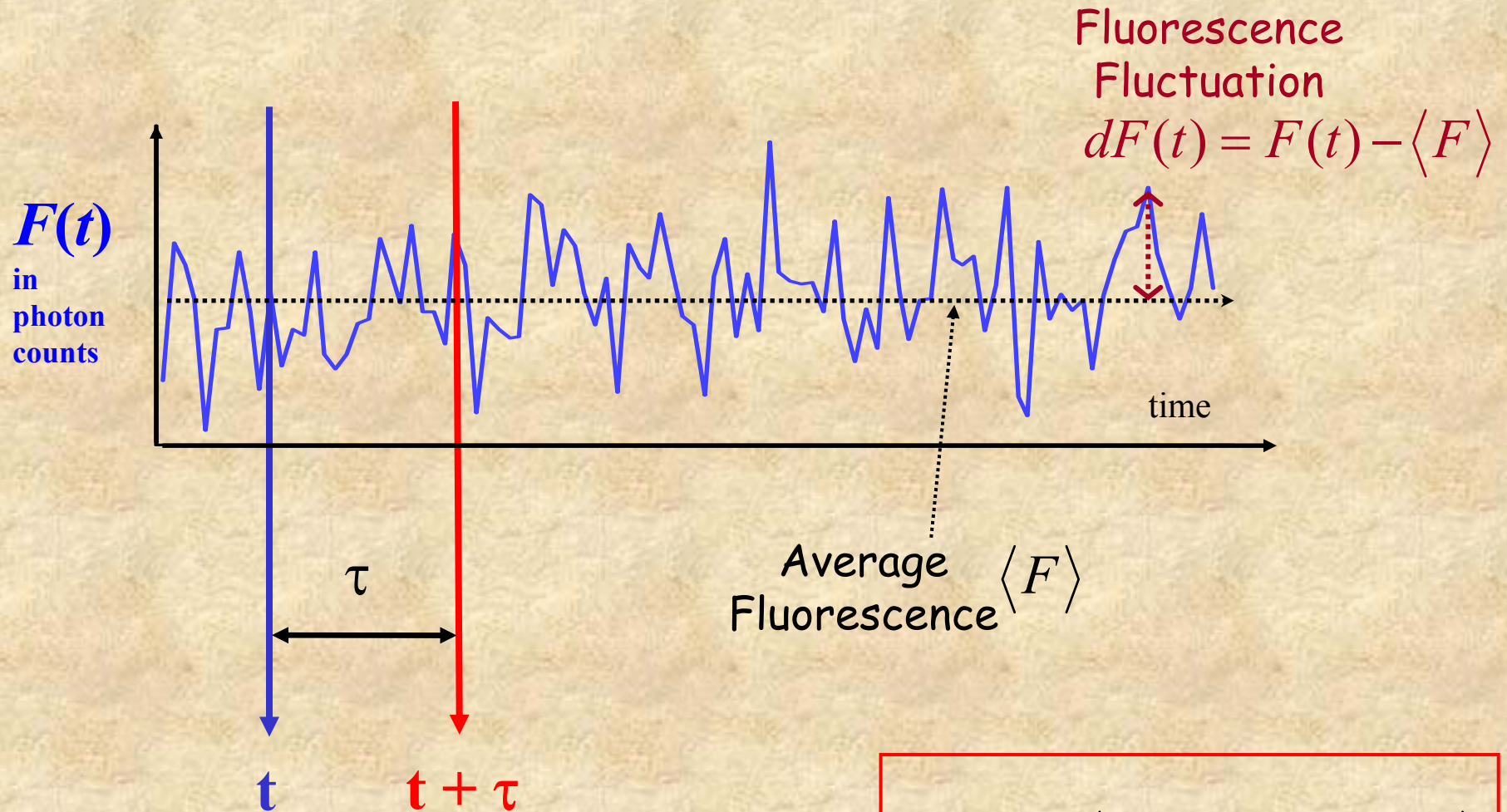
Photon Counting Histogram (PCH)



Autocorrelation Function:

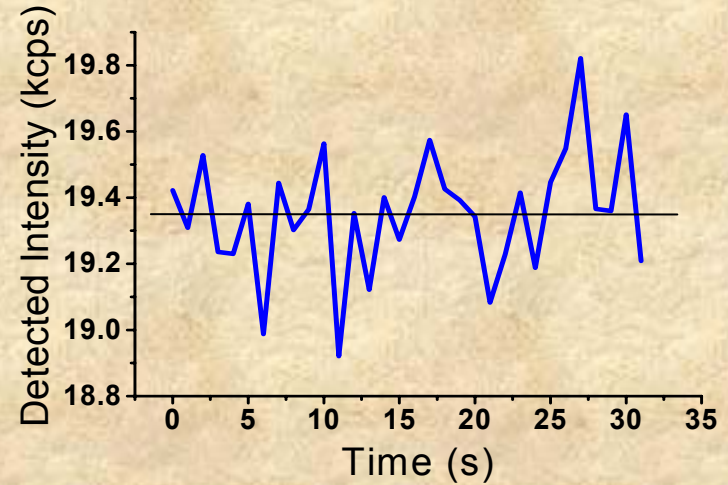
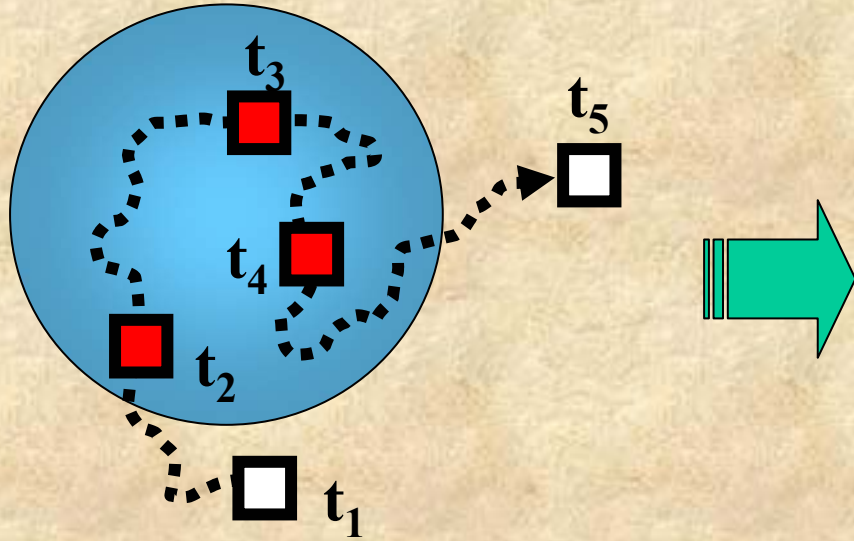
$$G(\tau) = \frac{\langle dF(t) \cdot dF(t + \tau) \rangle}{\langle F \rangle^2}$$

Calculating the Autocorrelation Function

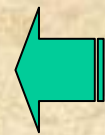
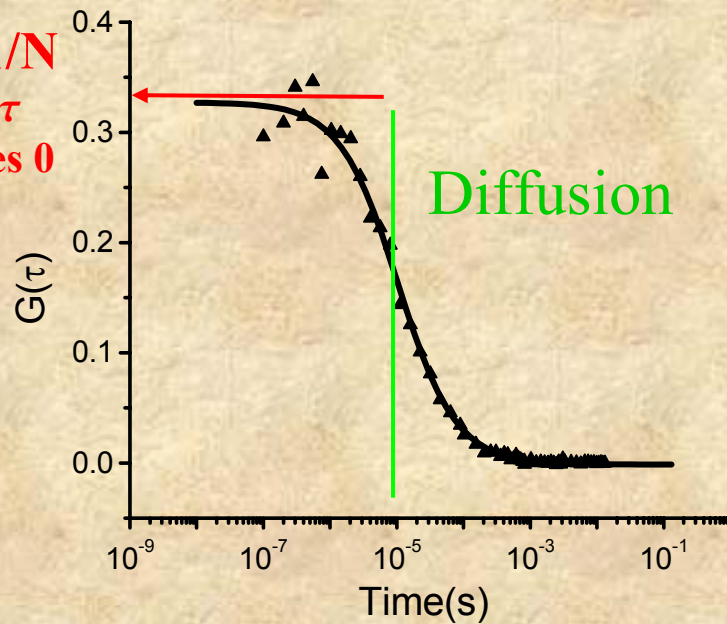


$$G(\tau) = \frac{\langle dF(t) \cdot dF(t + \tau) \rangle}{\langle F \rangle^2}$$

The Autocorrelation Function



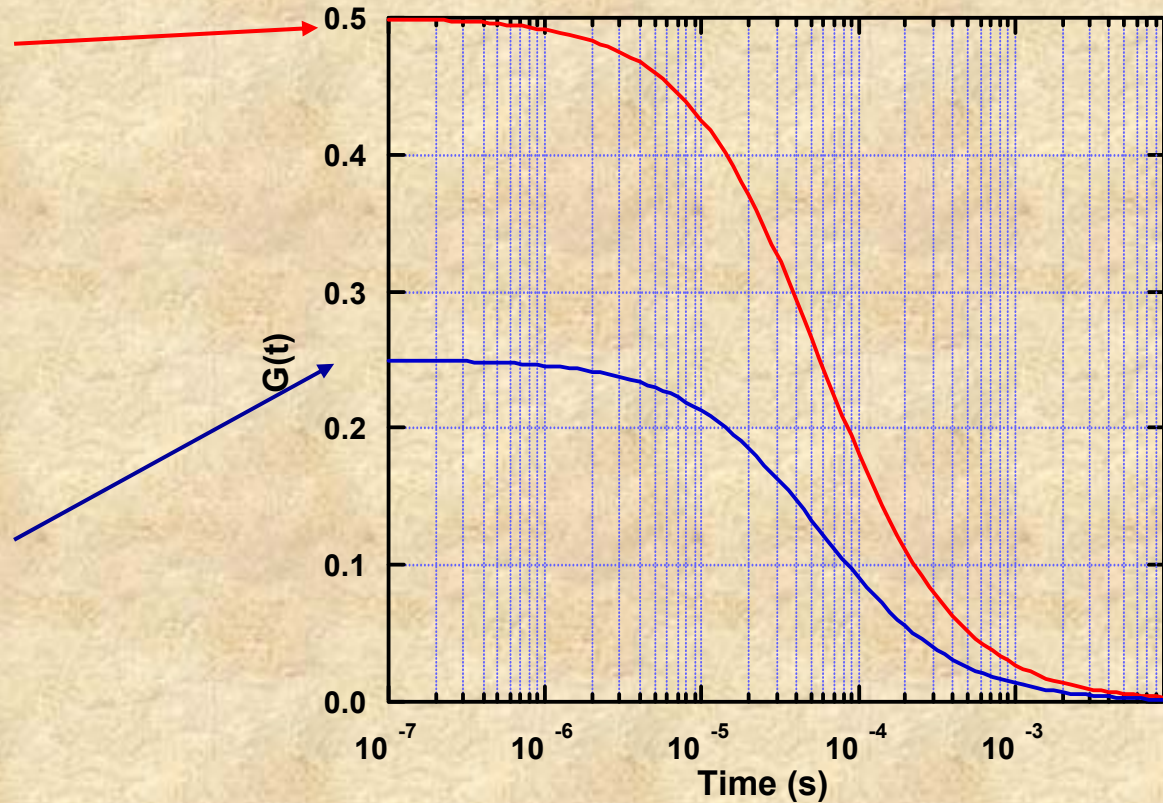
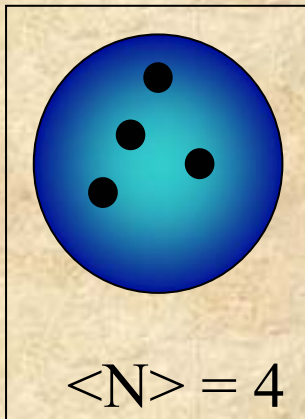
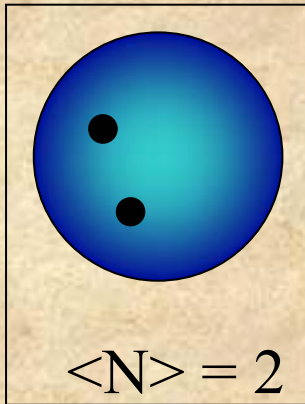
$G(0) \propto 1/N$
as time τ
approaches 0



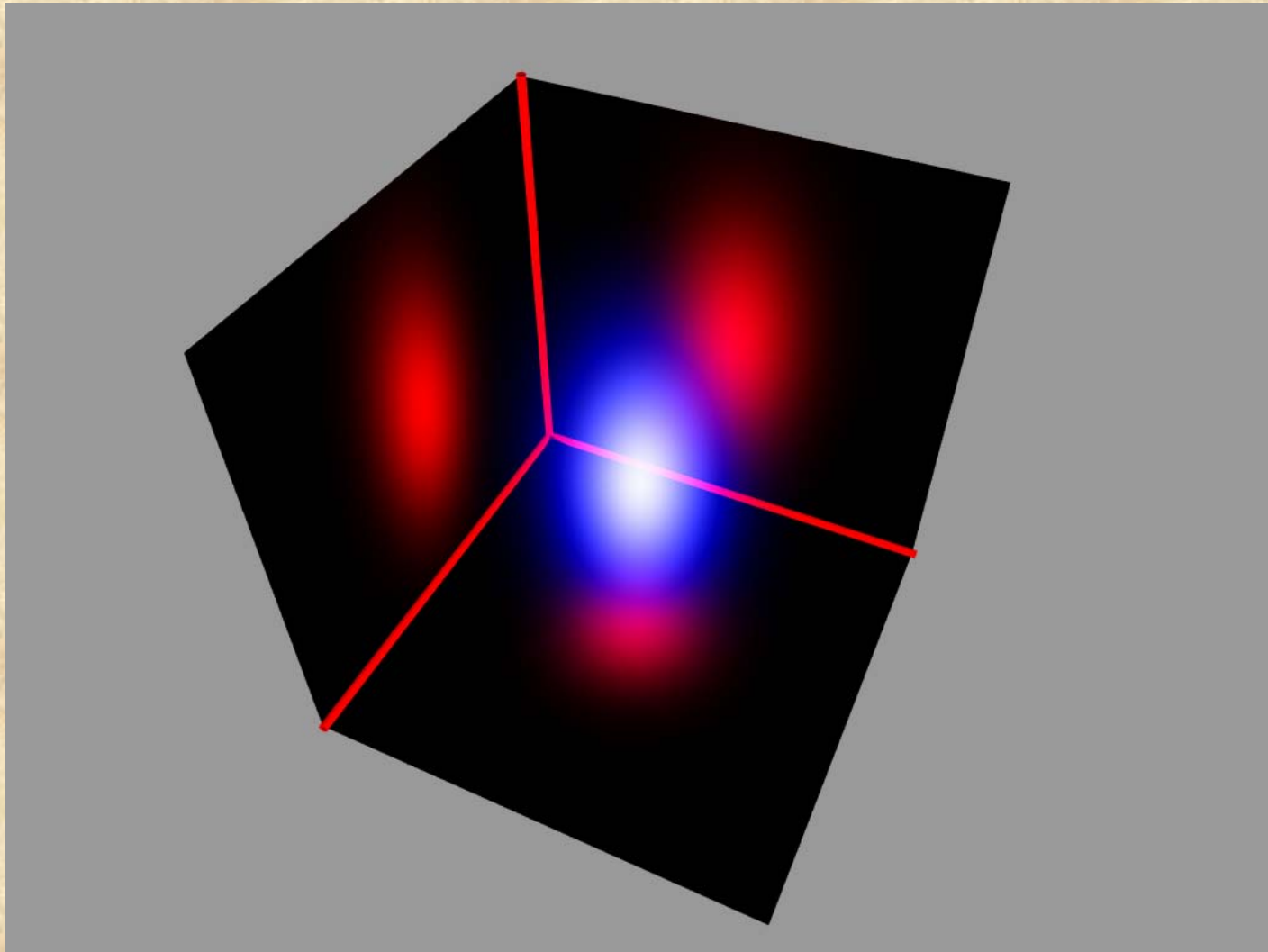
$$G(\tau) = \frac{\langle dF(t) dF(t + \tau) \rangle}{\langle F \rangle^2}$$



The Effects of Particle Concentration on the Autocorrelation Curve



What about the excitation (or observation) volume shape?



Correlation function of diffusing molecules

For a 3-dimensional Gaussian excitation volume:

$$G(\tau) = \frac{1}{\sqrt{8}} \frac{1}{N} \left(1 + \frac{8D\tau}{w_0^2} \right)^{-1} \left(1 + \frac{8D\tau}{z_0^2} \right)^{-1/2}$$

1-photon equation
contains a 4,
instead of 8

- N: average number of particles inside volume
- D: Diffusion coefficient
- w_0 : radial beam waist of two-photon laser spot
- z_0 : axial beam waist of two-photon laser spot

The Effects of Particle Size on the Autocorrelation Curve

Diffusion Constants

300 $\mu\text{m}^2/\text{s}$

90 $\mu\text{m}^2/\text{s}$

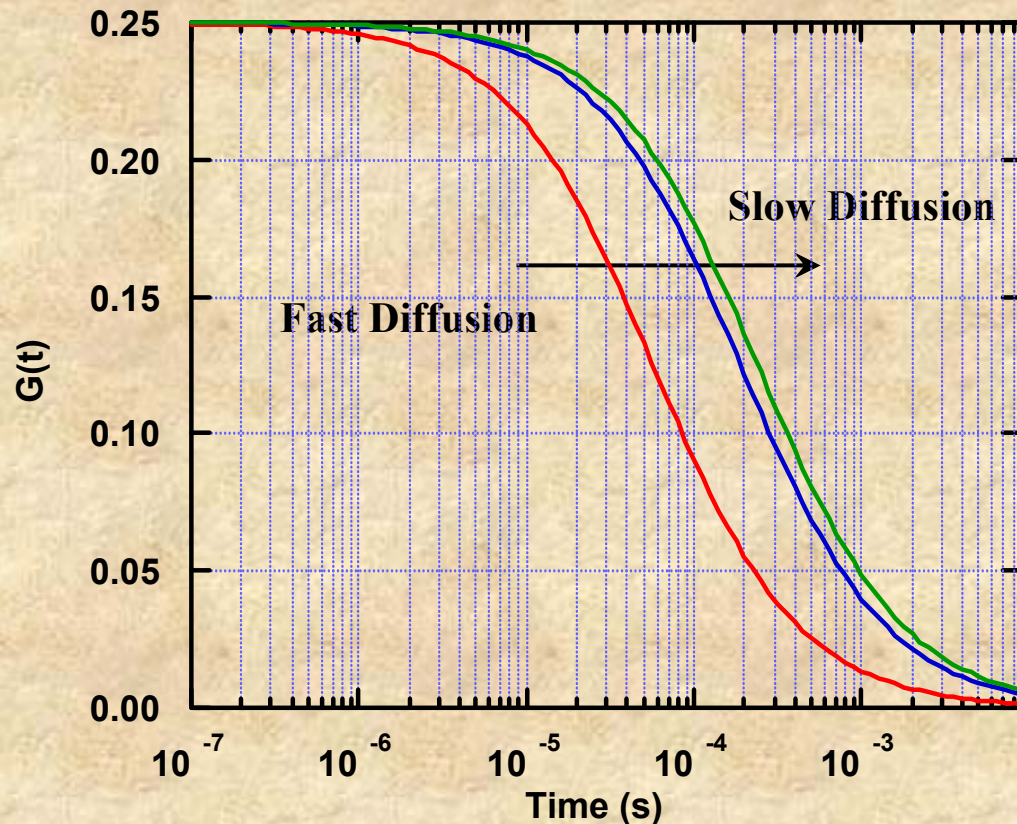
71 $\mu\text{m}^2/\text{s}$

Stokes-Einstein Equation:

$$D = \frac{k \cdot T}{6 \cdot \pi \cdot \eta \cdot r}$$

and

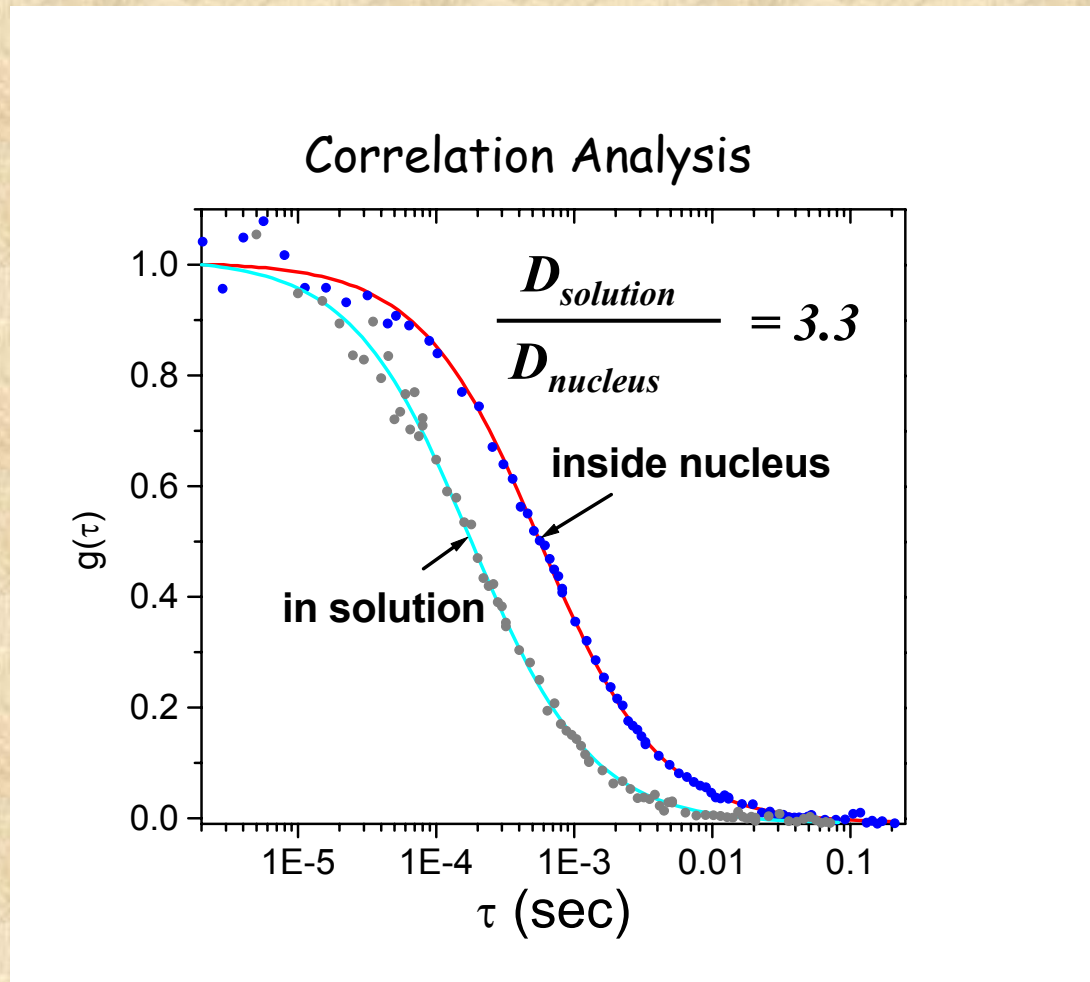
$$MW \propto \text{Volume} \propto r^3$$



Monomer \rightarrow Dimer

Only a change in D by a factor of $2^{1/3}$, or 1.26

FCS inside living cells

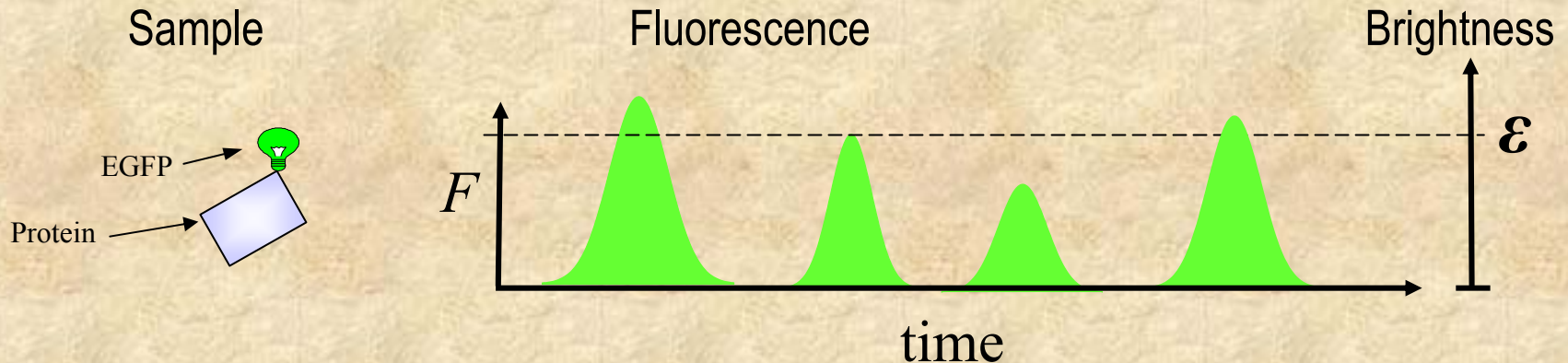


Measure the diffusion coefficient of Green Fluorescent Protein (GFP) in aqueous solution in inside the nucleus of a cell.

Statistical Analysis: Brightness

Brightness ϵ is the **average fluorescence intensity** of a single particle

Illustration:

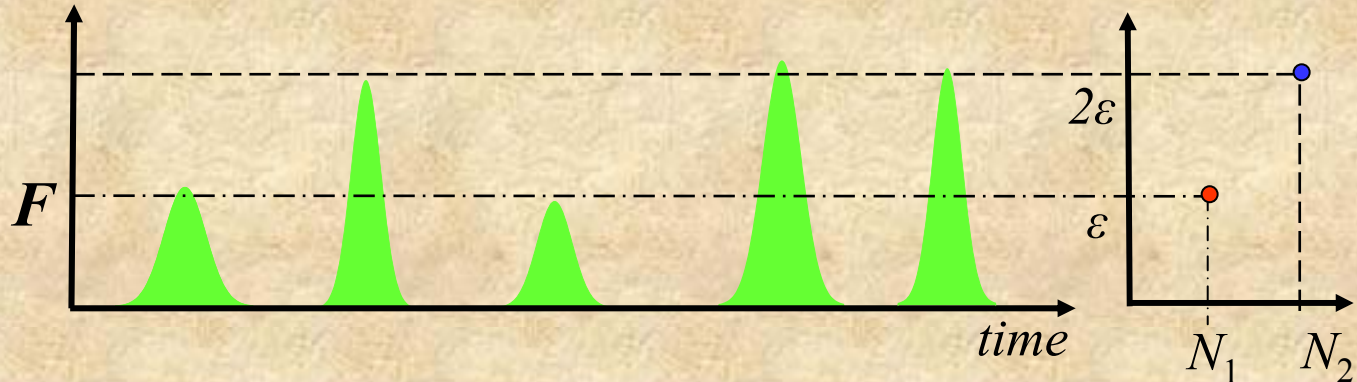
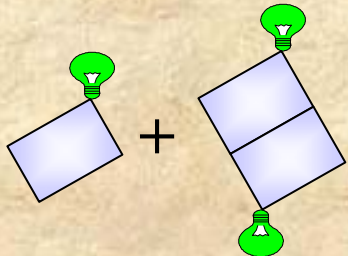
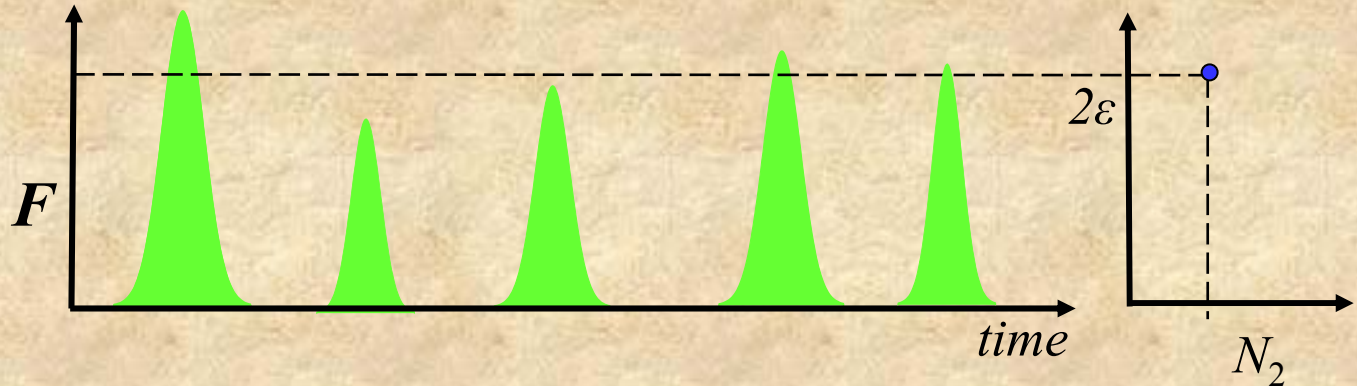
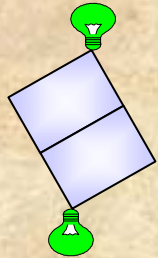
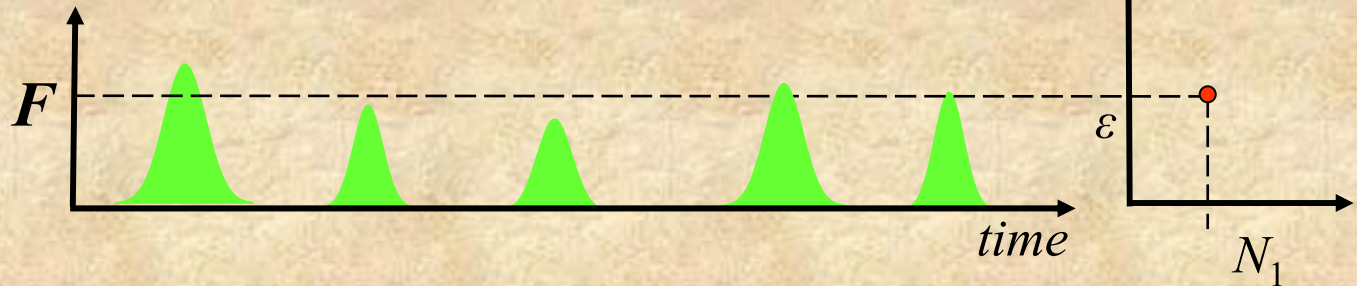
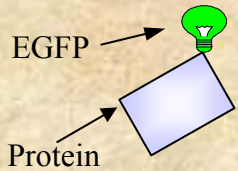


Brightness Encodes Stoichiometry

Sample

Fluorescence

Brightness



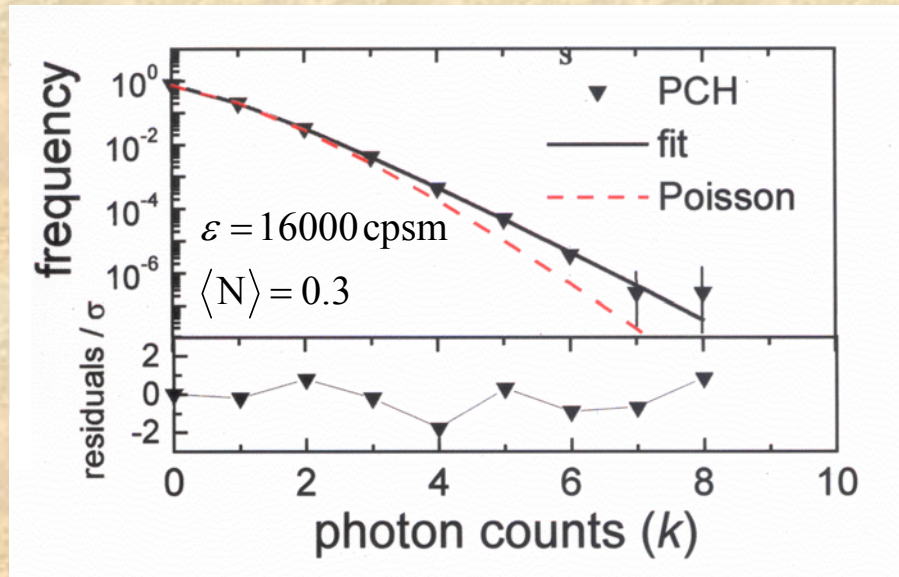
Photon Counting Histogram (PCH)

Aim: To resolve species from differences in their molecular brightness

Molecular brightness ε : The average photon count rate of a single fluorophore

PCH: probability distribution function $p(k)$

where $p(k)$ is the probability of observing k photon counts



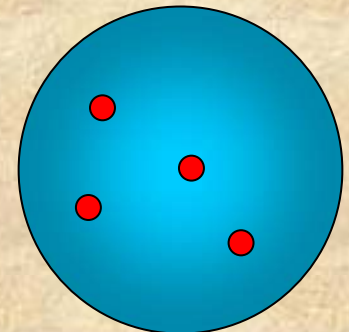
Single Species:

$$p(k) = PCH(\varepsilon, \langle N \rangle)$$

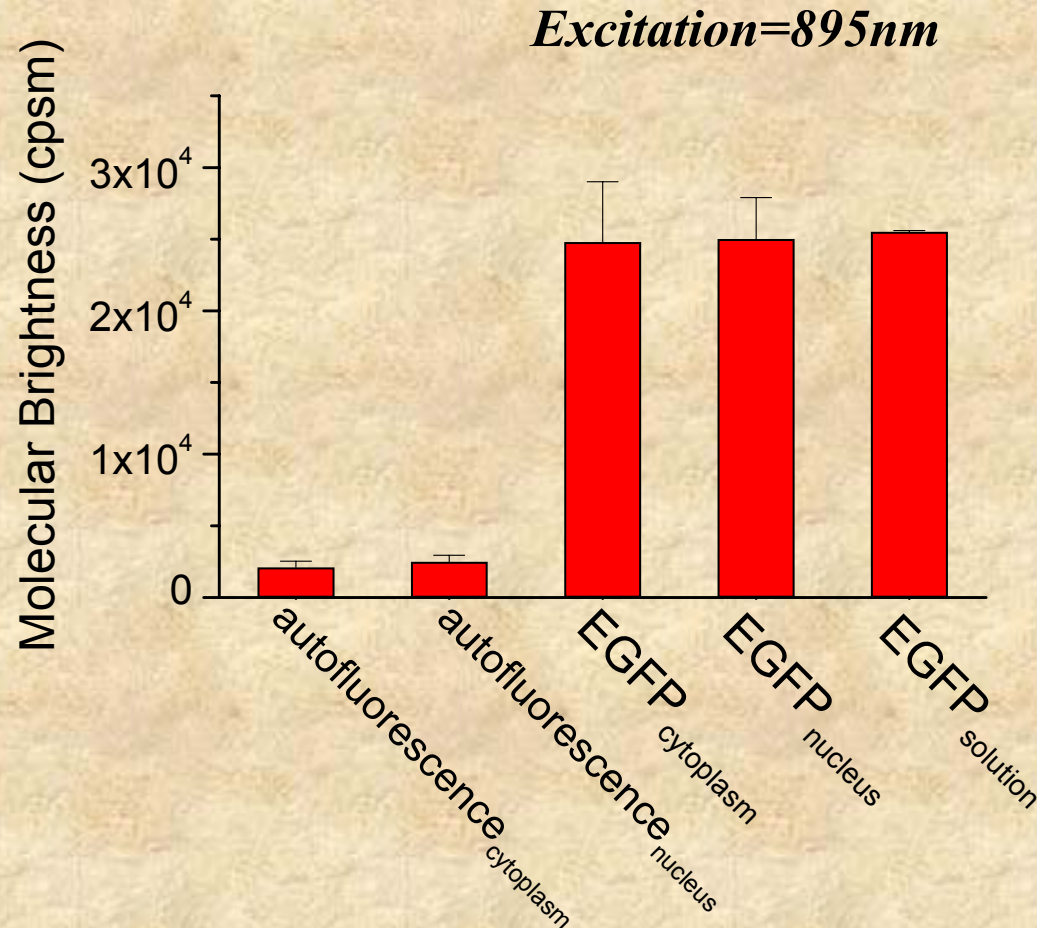
Note: PCH is Non-Poissonian!

Sources of Non-Poissonian Noise

- Detector Noise
- Diffusing Particles in an Inhomogeneous Excitation Beam*
- Particle Number Fluctuations*
- Multiple Species*

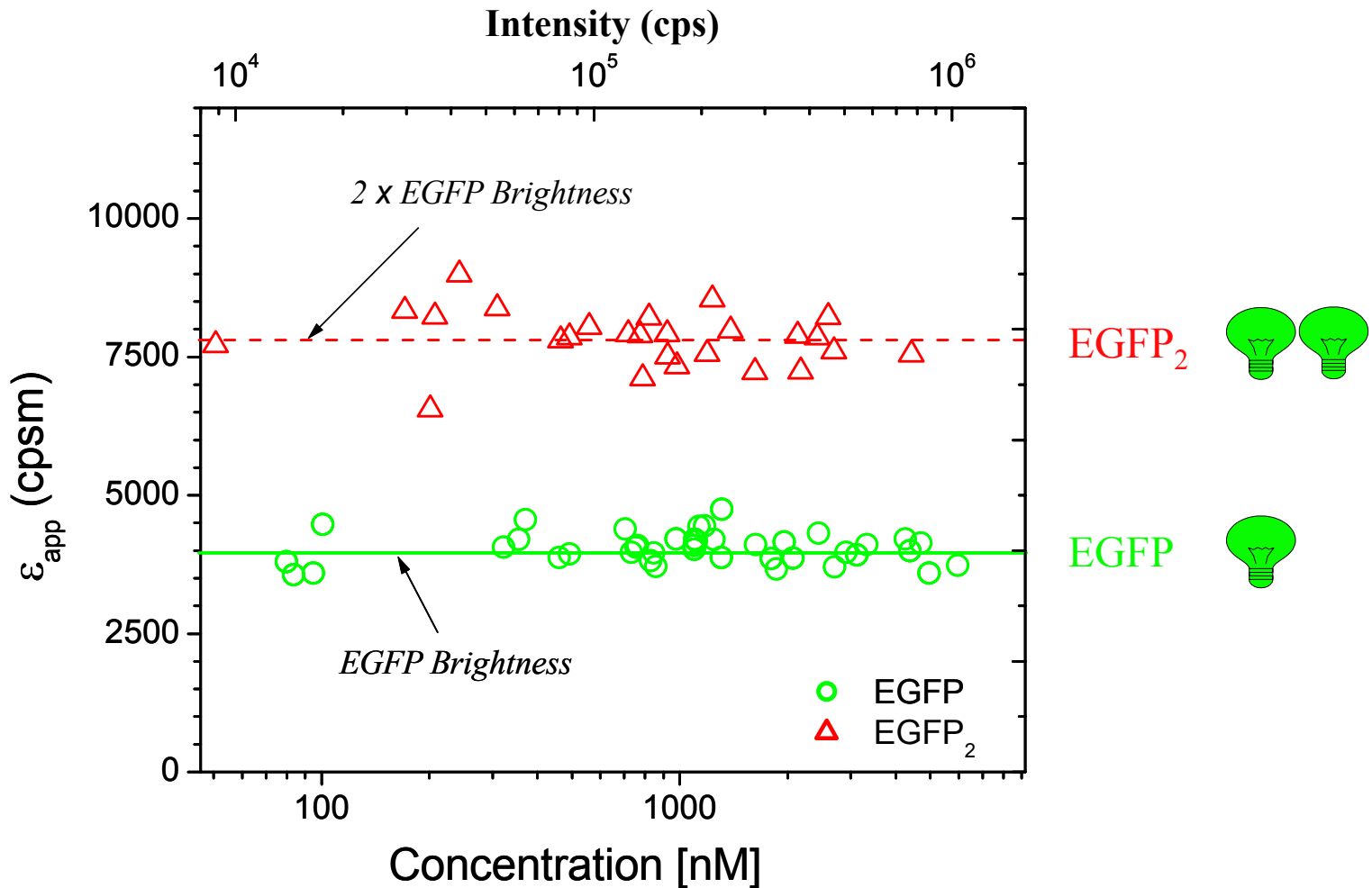


PCH in cells: Brightness of EGFP



*The molecular brightness of EGFP is a factor **ten** higher than that of the autofluorescence in HeLa cells*

Brightness and Stoichiometry



Brightness of EGFP₂ is twice the brightness of EGFP

The End